

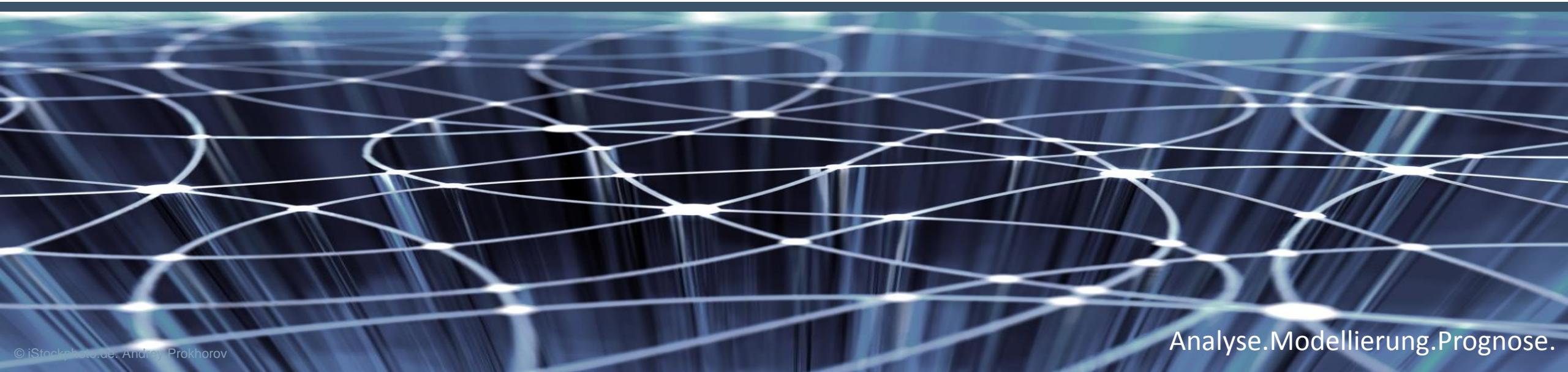


**STASA**  
Steinbeis Angewandte  
Systemanalyse GmbH

**Universität Stuttgart**  
**II. Institut für Theoretische Physik**

# Individual Decisions, Innovations and Sustainable Economics

Günter Haag



Analyse.Modellierung.Prognose.

## One fundamental stimulus of human research



“Dass ich nicht mehr mit saurem Schweiß  
rede von dem was ich nicht weiß

(sondern)

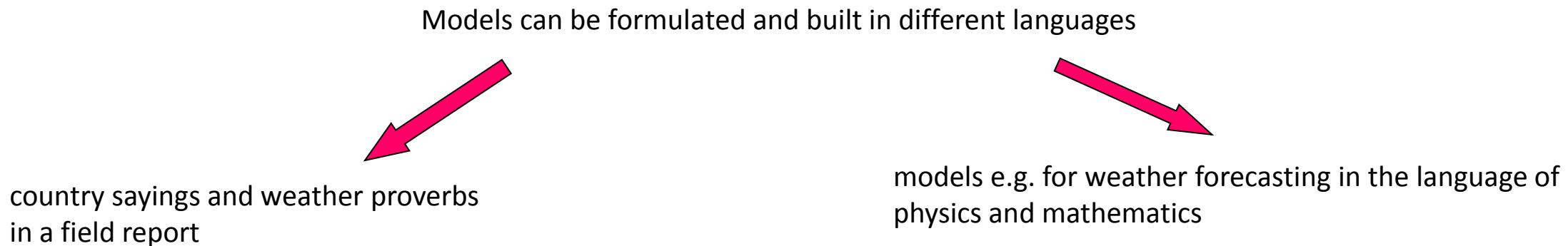
Dass ich erkenne, was die Welt  
im Innersten zusammenhält” (Goethe, Faust I)

“What holds the world together at its core”

Douglas Adams (1979) formulated in his famous book “The Ultimate Hitchhiker’s Guide to the Galaxy” in a simple but realistic way, ...where do we come from, where do we go and where do we get the best Wiener Schnitzel?

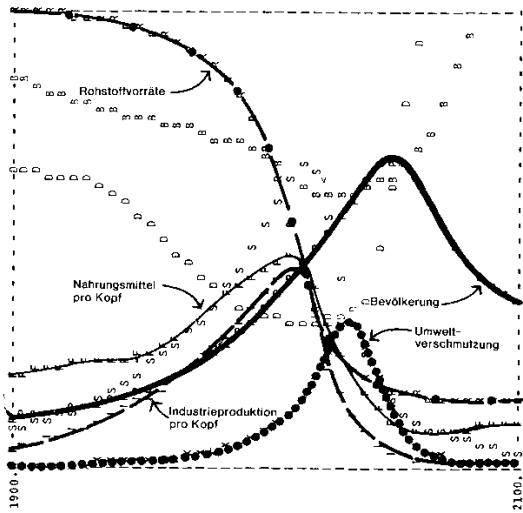
# What is a model?

Models are based on rules  
Rules are based on experience  
John L. Casti



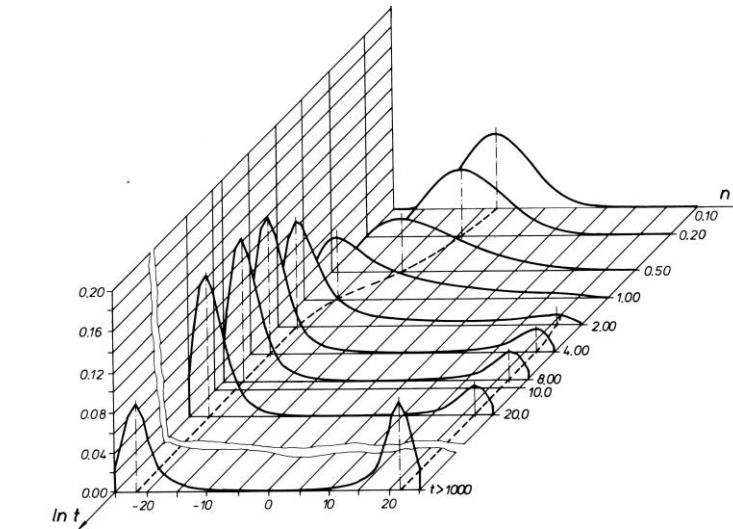
The model should be kept as simple as possible but not too simple  
Albert Einstein

## Deterministic Models

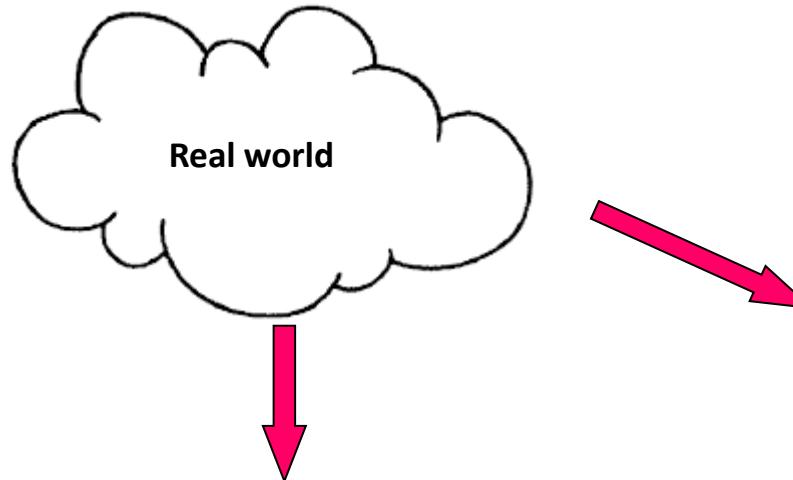


**Club of Rome (1972)**  
 System Dynamics (Jay Forrester)

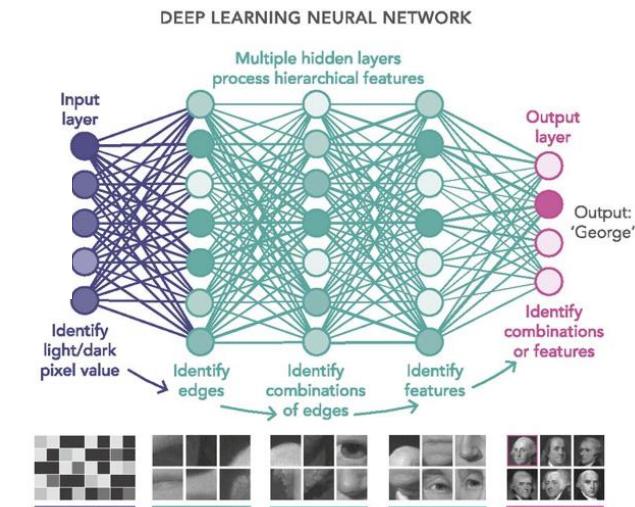
**MIT Boston (1990)**  
 World model (about 160.000 equations,  
 95% of the world economy)

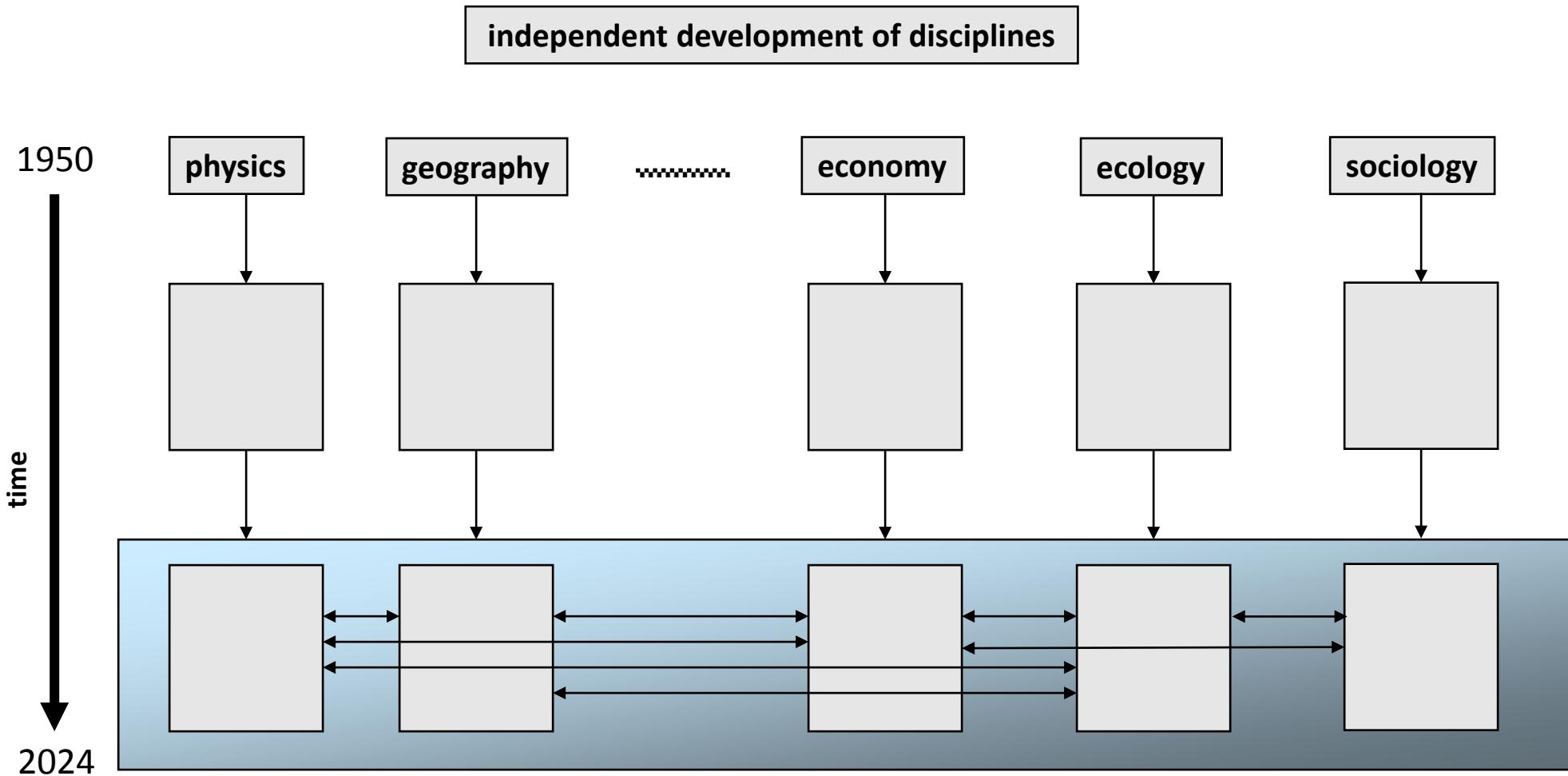


## Statistical Models models with uncertainties

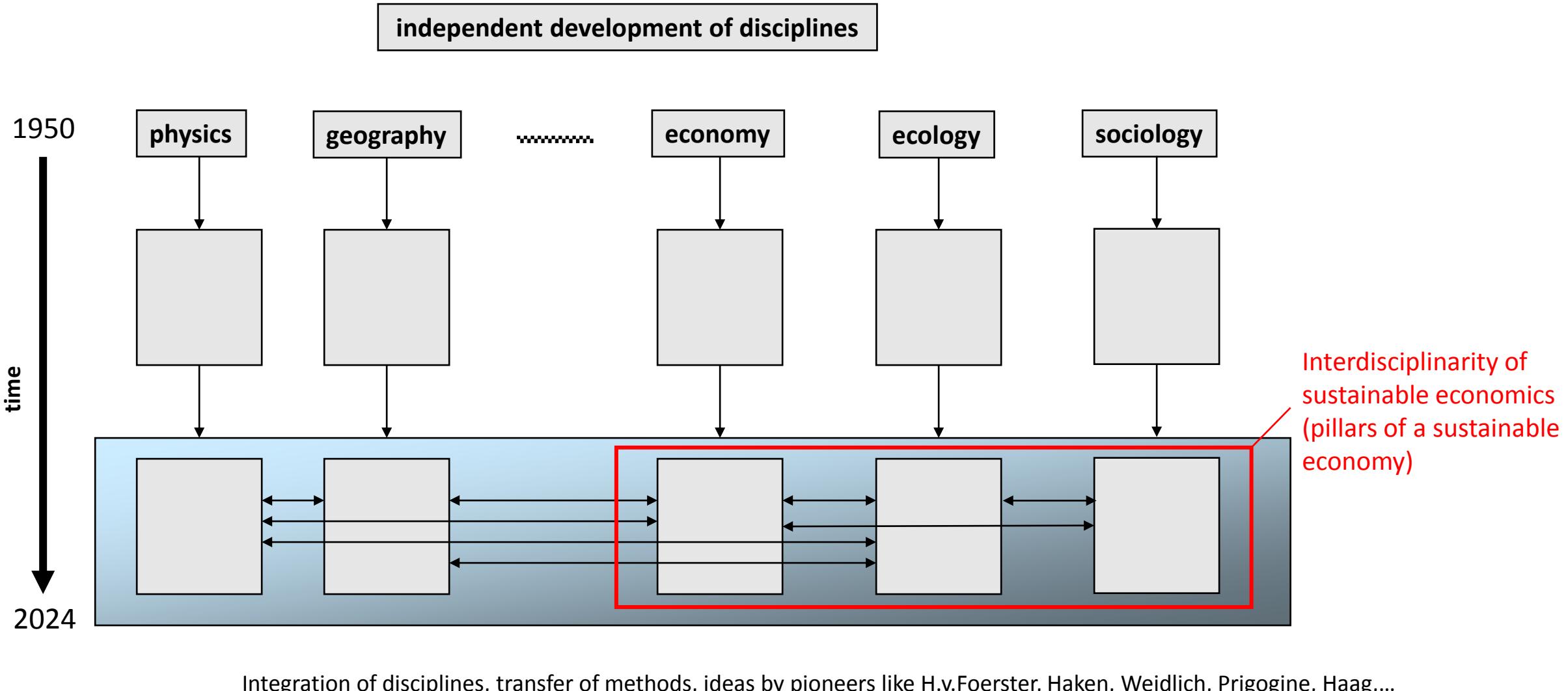


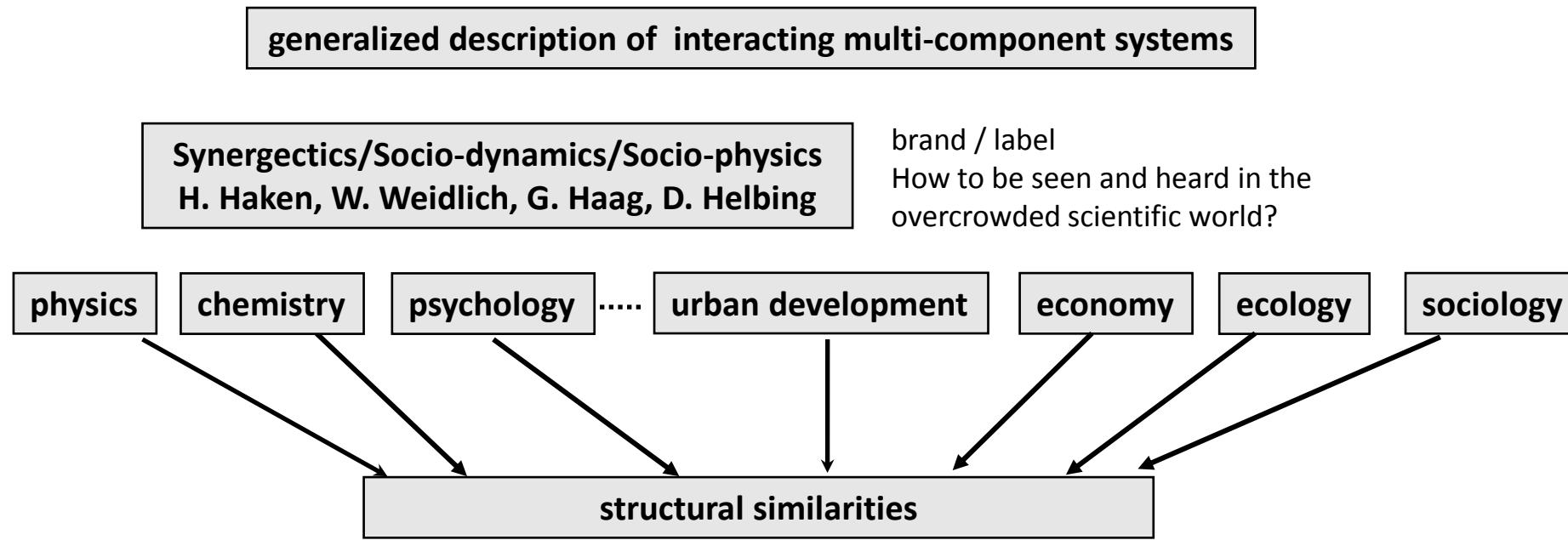
## Neural Networks (AI) data driven modelling



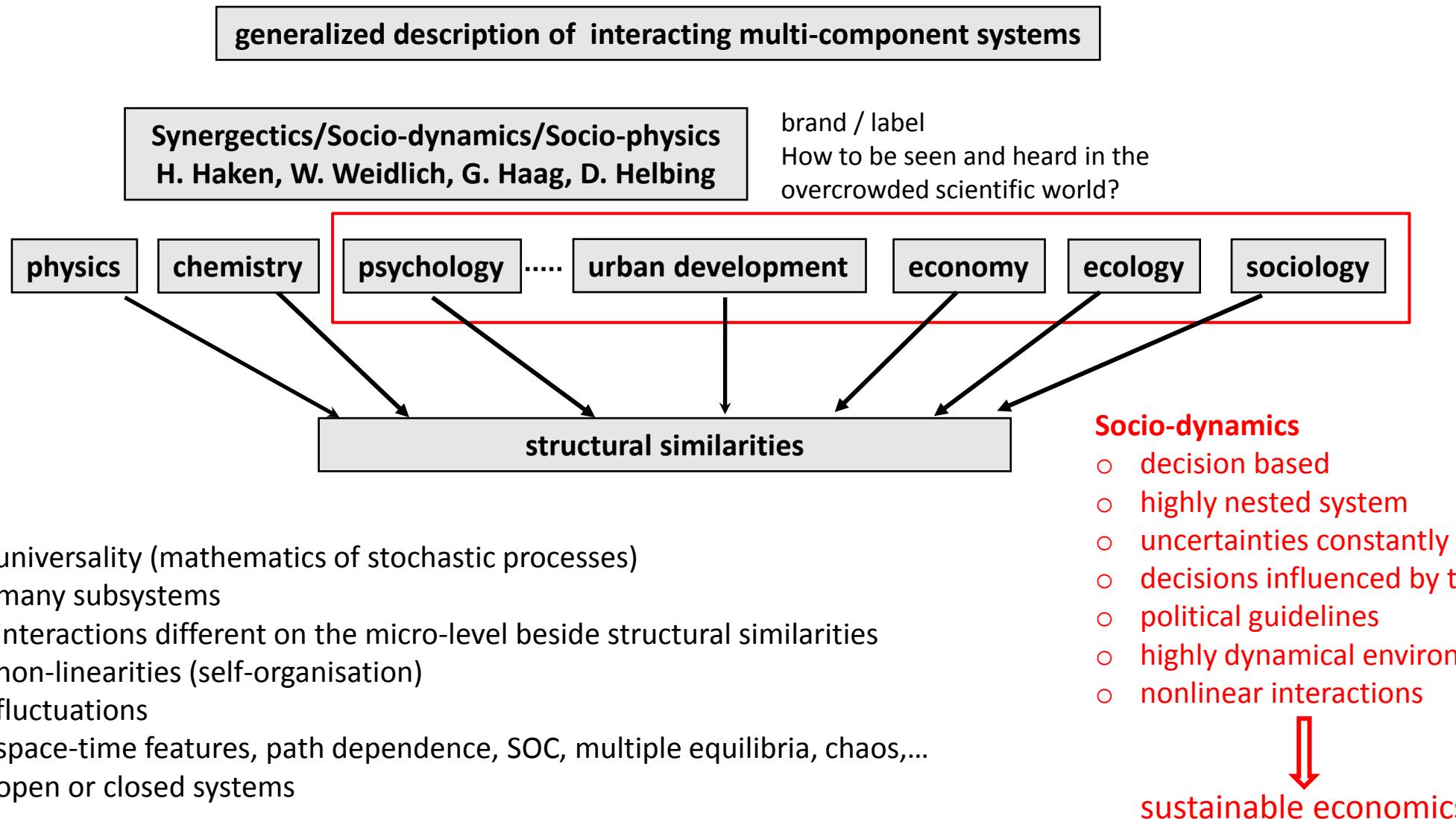


Integration of disciplines, transfer of methods, ideas by pioneers like H.v.Foerster, Haken, Weidlich, Prigogine, Haag,...

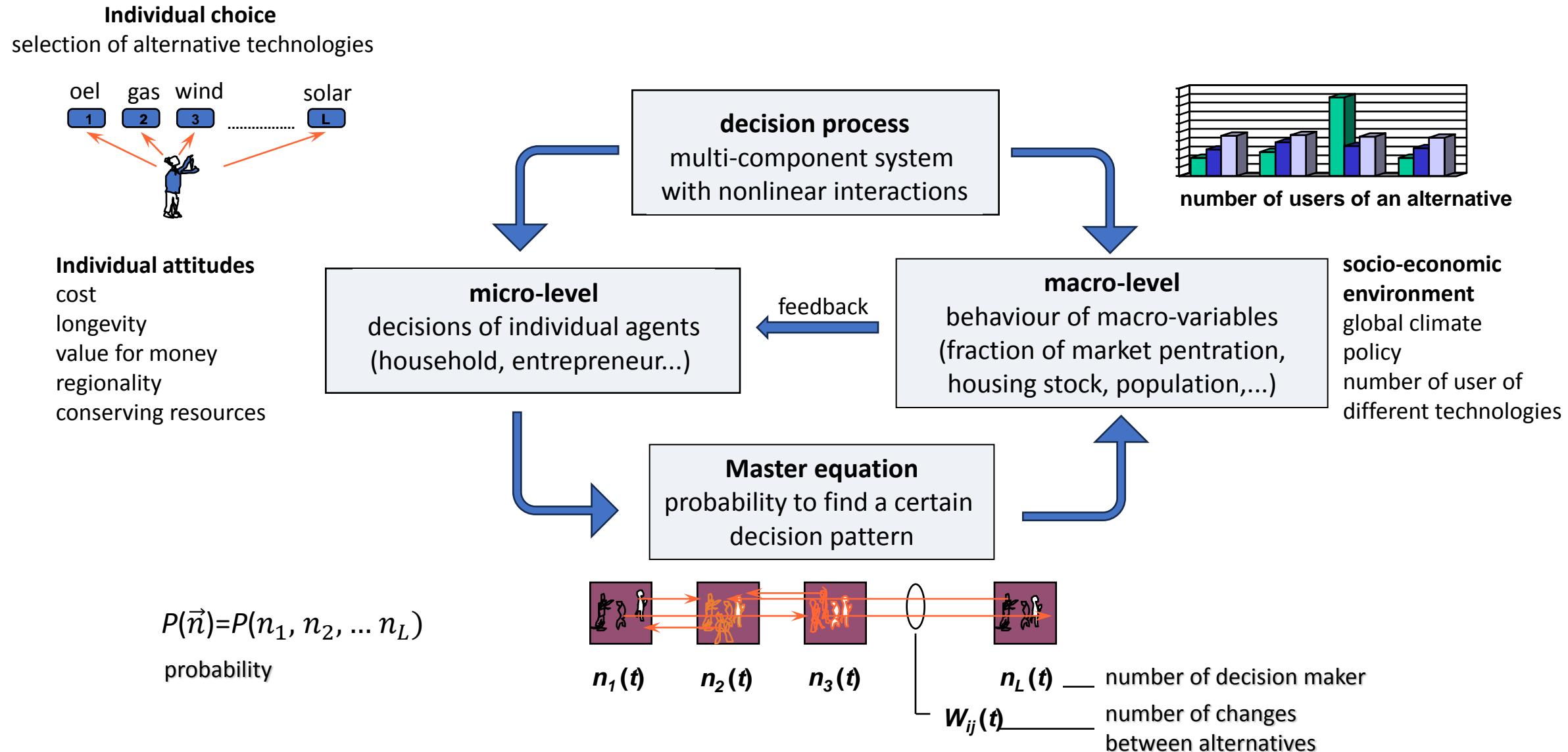


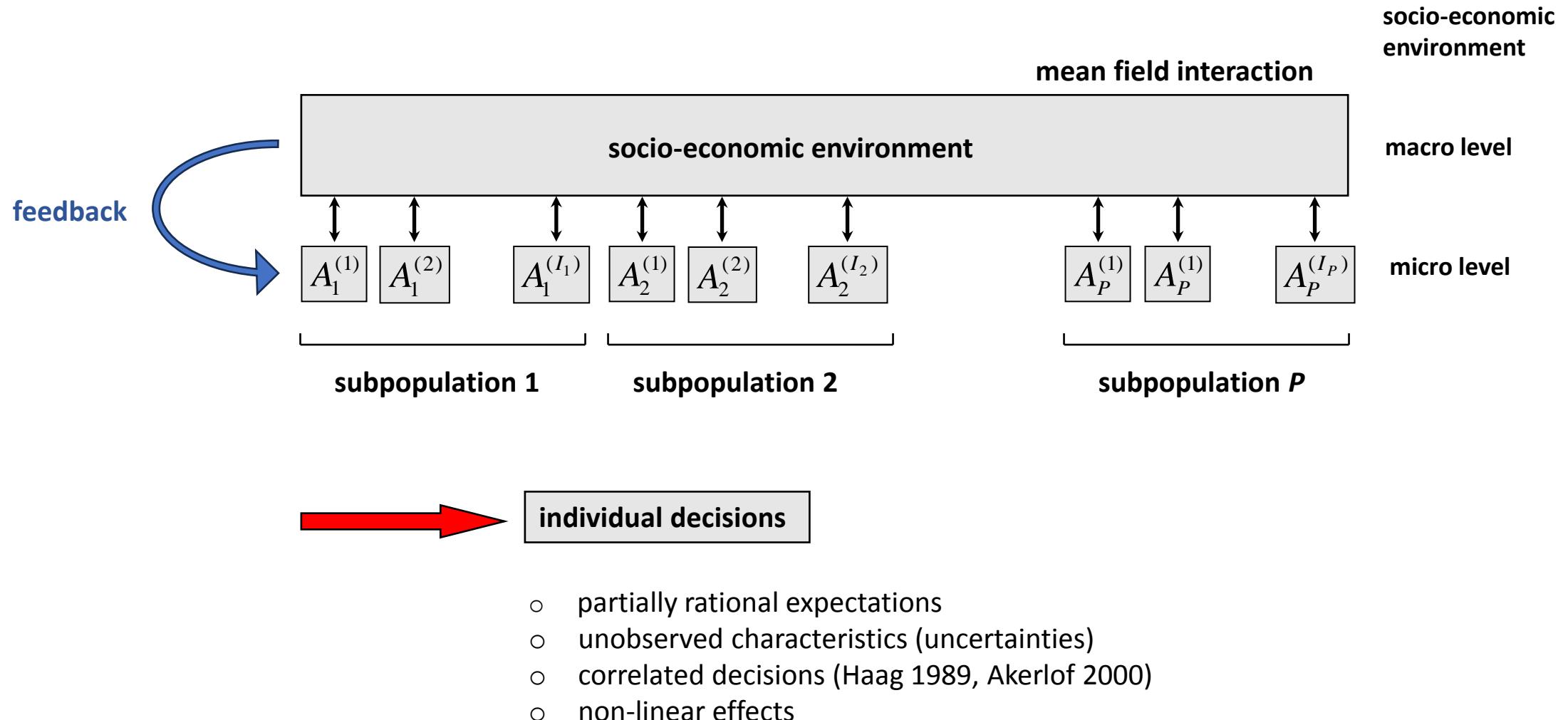


- universality (mathematics of stochastic processes)
- many subsystems
- interactions different on the micro-level beside structural similarities
- non-linearities (self-organisation)
- fluctuations
- space-time features, path dependence, SOC, multiple equilibria, chaos,...
- open or closed systems

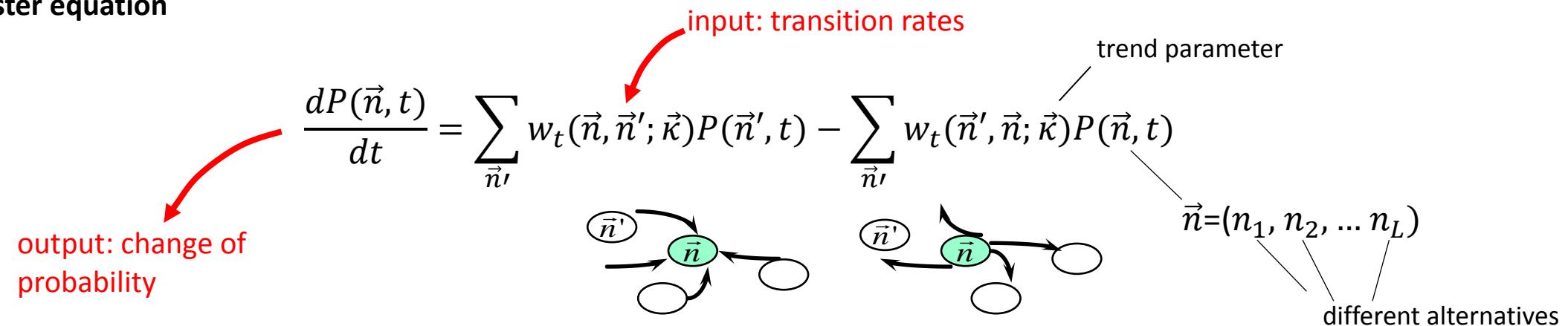


# How to model Decision Processes – The Framework



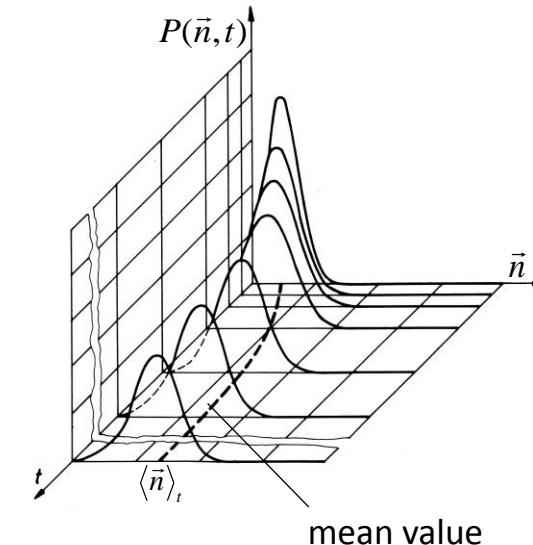


## Pauli Master equation



### Some properties

- The transition rates define the process – all we need
- dynamic equation for probability to find a certain configuration
- → Mean value equation, variance equation
- balance equation for probability fluxes
- irreversible dynamics → unique stationary state
- Markoff assumption → socio-dynamics: system parameters change over time
- Master equation → Agent-Based-Modelling, Fokker-Planck-Equation



## Error minimization

$$F[\vec{\kappa}] = \sum_t \sum_{\vec{n}, \vec{k}} \{w_t^e(\vec{n}, \vec{n}') - w_t(\vec{n}, \vec{n}'; \vec{\kappa})\}^2 = \min$$

|  
 empirical data      model data

## Equations of motion

$$\frac{d\overline{n(t)}}{dt} = \sum_{\vec{n}} \vec{n} \frac{dP(\vec{n}, t)}{dt} = \frac{d}{dt} \sum_{\vec{n}} \vec{n} P(\vec{n}, t)$$



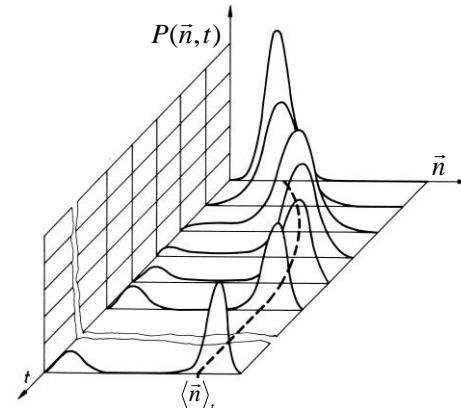
optimal estimation of  
system parameters

input of  
parameters

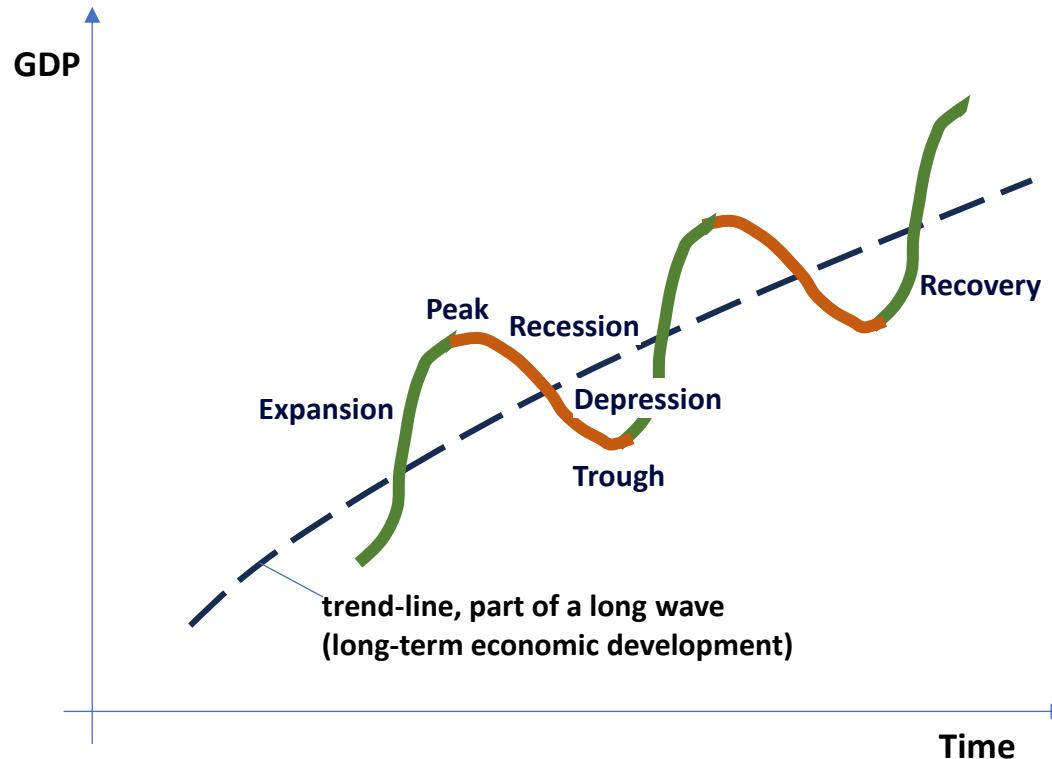
non-linear system of difference  
equations for the mean values

different  
scenarios

forecasting of the mean behaviour  
of the trajectories



# 1. Example: Business Cycles – Theory of Investments



## Business cycle (4 to 6 years)

cycle of fluctuations in the Gross Domestic Product (GDP) around its long-term natural development

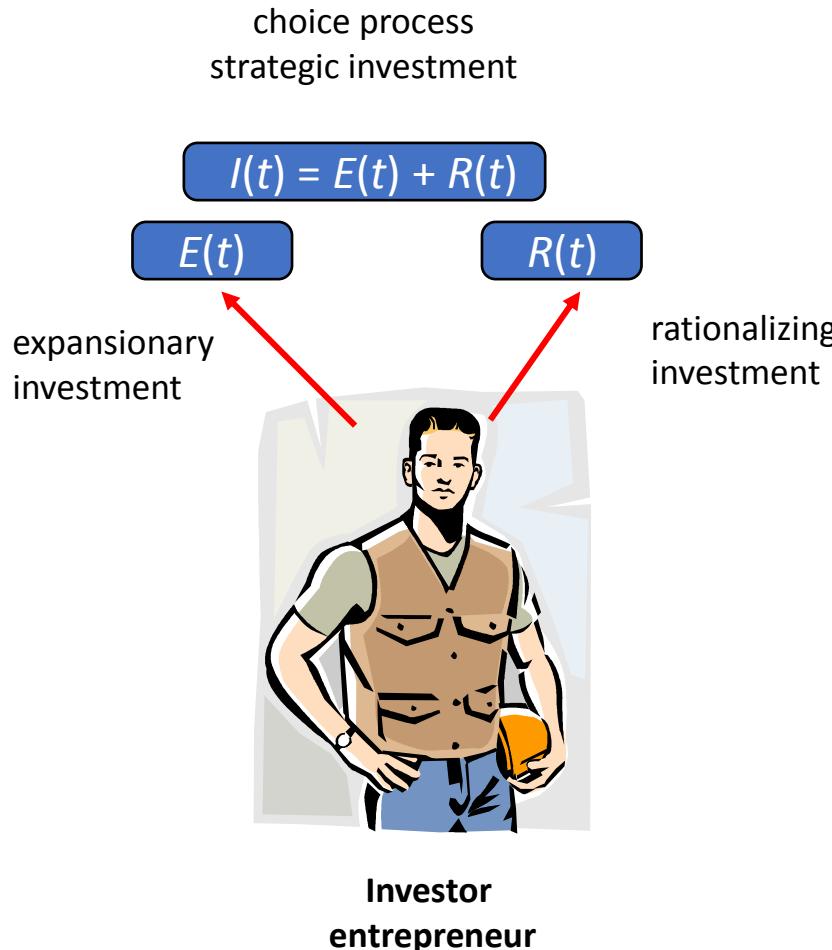
- Expansion
- Peak
- Recession
- Depression
- Trough
- Recovery

## Observation at trade fairs:

years nothing new – years all have new coordination of firms activities (information exchange)  
→ collective behaviour

How can we eliminate business cycles (Tinbergen, 1983)?

Business cycles and fluctuations around the trend line are natural – we have to anticipate its development (Haag)



### **Sectoral restrictions**

„Schumpeter goods sector“ – parts of industry and public sector operating similar to industrial organisations

### **Spatial restrictions**

Fokus on statistical units such as whole nations, states or regions

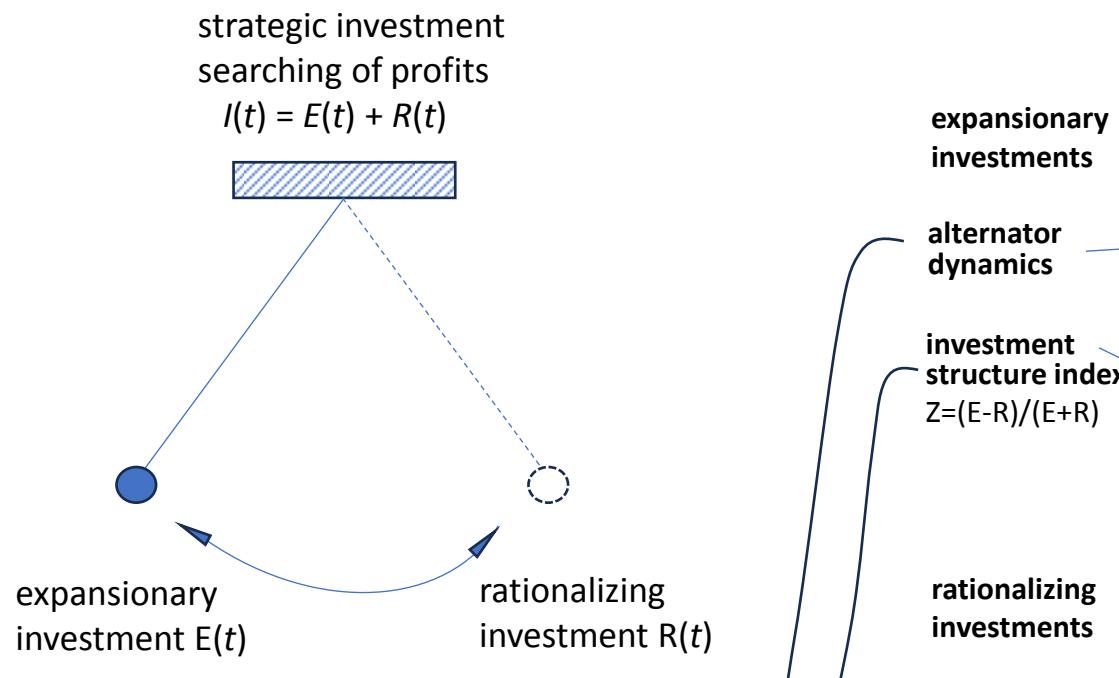
### **Functional restrictions**

Fokus on industrial investor and his strategic behaviour under rivalry

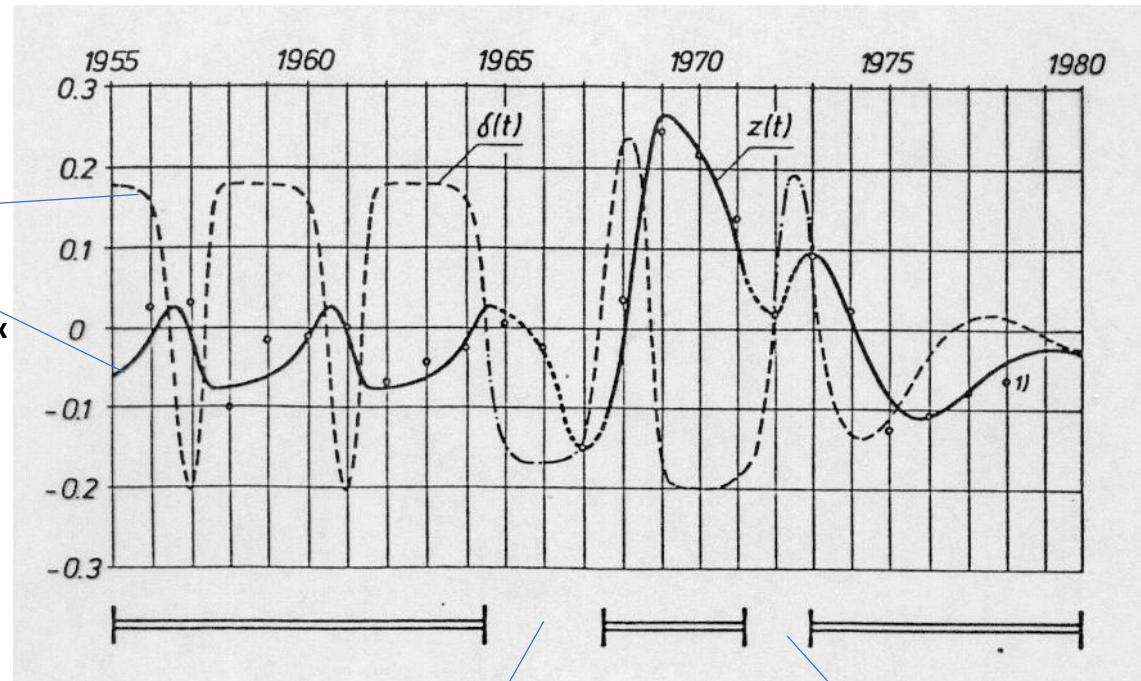
### **Focus on supply side**

Demand side neglected, induced investment neglected  
(taken into account by Reiner Koblo, 1991)

# Schumpeter Clock (Mensch, Weidlich, Haag, 1981)



**Data Base: IfO-Data about firms investment**  
of about 6.000 firms



**How much do I want to invest (next period)**

**How much did I invest (last period)**

## Schumpeter Clock – The transition rates

Suppose number of investors is categorized in *R*-type investor  $n_R(t)$  and *E*-type investors  $n_E(t)$   
 Total number of investors is  $2N$  (constant)

$$n_E + n_R = 2N \quad \text{constant}$$

$$n_E - n_R = 2n \quad \text{relevant variable}$$

$$n_E = N + n$$

$$n_R = N - n$$

**transitions between decision configurations**

$$\{n_E, n_R\} \longrightarrow \{n_E + 1, n_R - 1\}$$

$$\{n_E, n_R\} \longrightarrow \{n_E - 1, n_R + 1\}$$

$$n \longrightarrow n + 1$$

$$n \longrightarrow n - 1$$

**number of transitions per time unit between configurations**

$$w_{\uparrow}(n) = w(n \rightarrow n + 1) = n_R p_{RE}(n) = (N - n)\nu \exp(u(n_E) - u(n_R))$$

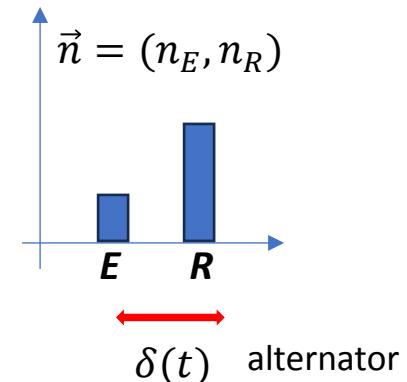
$$w_{\downarrow}(n) = w(n \rightarrow n - 1) = n_E p_{ER}(n) = (N + n)\nu \exp[-(u(n_E) - u(n_R))]$$

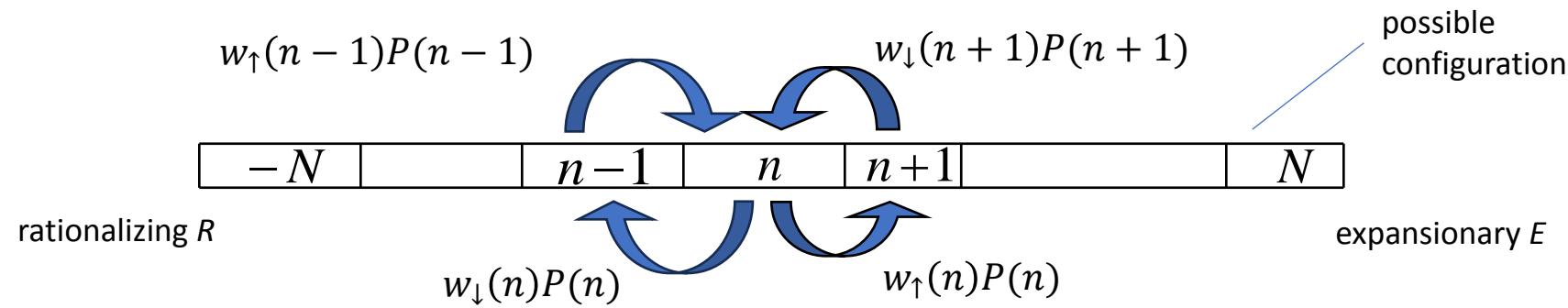
rate of change preference  
from *E* → *R*

frequency  
of switch

$\kappa n + \delta(t)$   
 coordinator  
 utility difference  
 alternator

**decision configuration**





## master equation

$$\frac{dP(n, t)}{dt} = w_{\downarrow}(n+1)P(n+1, t) + w_{\uparrow}(n-1)P(n-1, t) - (w_{\uparrow}(n) + w_{\downarrow}(n))P(n, t)$$

## stationary solution (exact)

detailed balance always fulfilled

$$w_{\downarrow}(n+1)P_{st}(n+1) = w_{\uparrow}(n)P_{st}(n)$$



$$P_{st}(n) = P_{st}(0) \prod_{m=1}^n \frac{w_{\uparrow}(m-1)}{w_{\downarrow}(m)}$$

$$x = n/N$$



$$x_s = \tanh(\delta + \kappa x_s)$$

lhs   rhs

calculation of mean value

$$\bar{n}(t) = \sum_{n=-N}^N n P(n, t) \quad \text{with} \quad \bar{x}(t) = \bar{n}(t)/N$$

equations of motion

investors configuration

$$\frac{d\bar{x}(t)}{dt} = 2\nu[\sinh(\delta(t) + \kappa\bar{x}(t)) - \bar{x}(t)\cosh(\delta(t) + \kappa\bar{x}(t))] \quad \longrightarrow \quad x_s = \tanh(\delta + \kappa x_s)$$

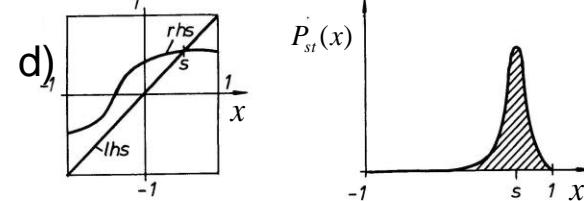
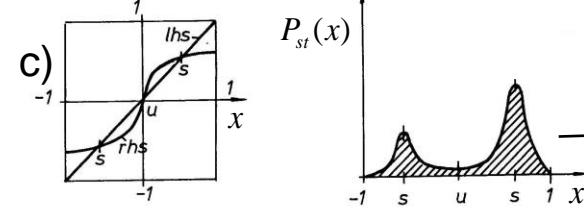
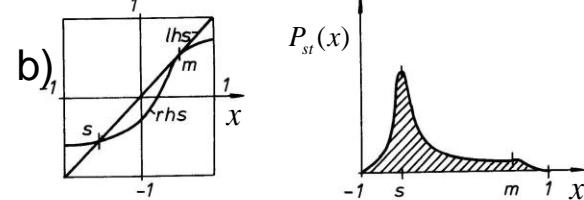
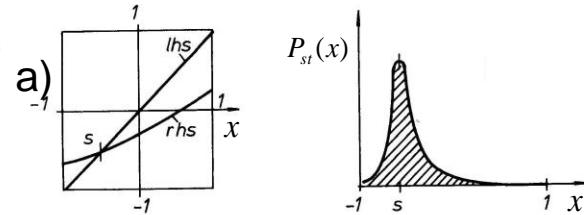
alternator dynamics

$$\frac{d\delta(t)}{dt} = -2\mu[\delta_0 \sinh(\beta\bar{x}(t)) + (\delta(t) - \delta_1) \cosh(\beta\bar{x}(t))]$$

 Static solutions, limit cycles

## Schumpeter Clock – German Data

$$x_s = \tanh(\delta(t) + \kappa x_s)$$

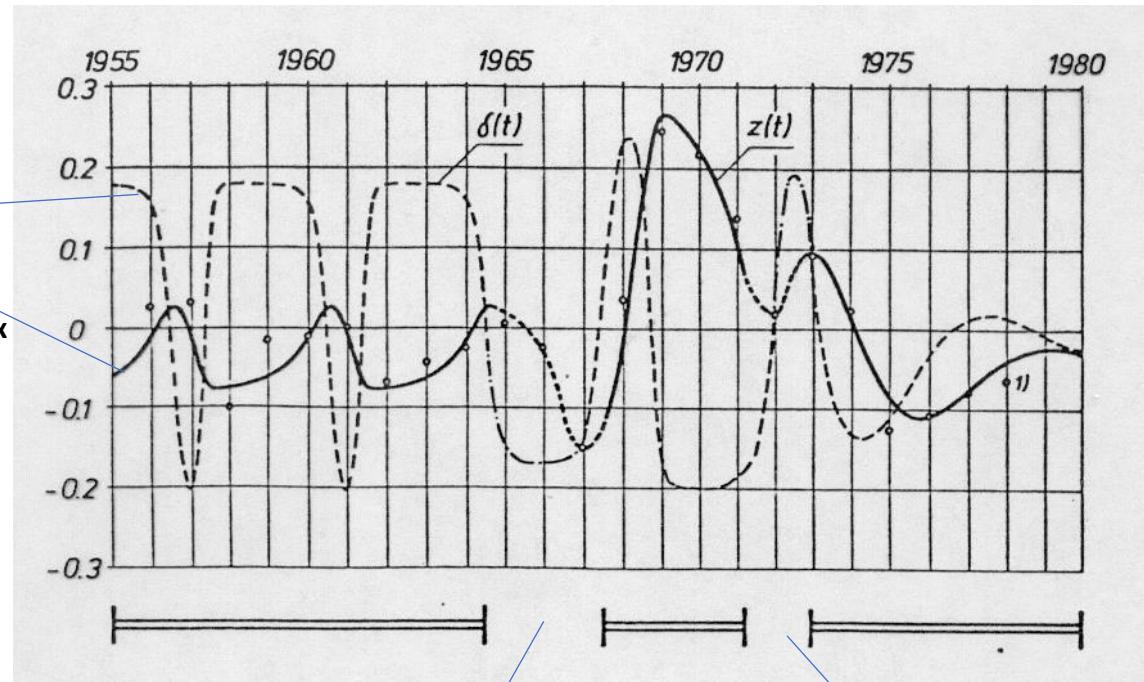


## expansionary investments

## alternator dynamics

## investment structure index

## rationalizing investments



hyperboom  
„Schiller“ effect  
Keynesian economist  
Grand coalition  
CDU+SPD

Two oil shocks caused  
slumpflation  
(M. Freedman)

# A few limitations

## Uncertainties

- uncertainties and outliers in the data
- uncertainties in the initial conditions
- uncertainties in the parameter estimation

## Complexity

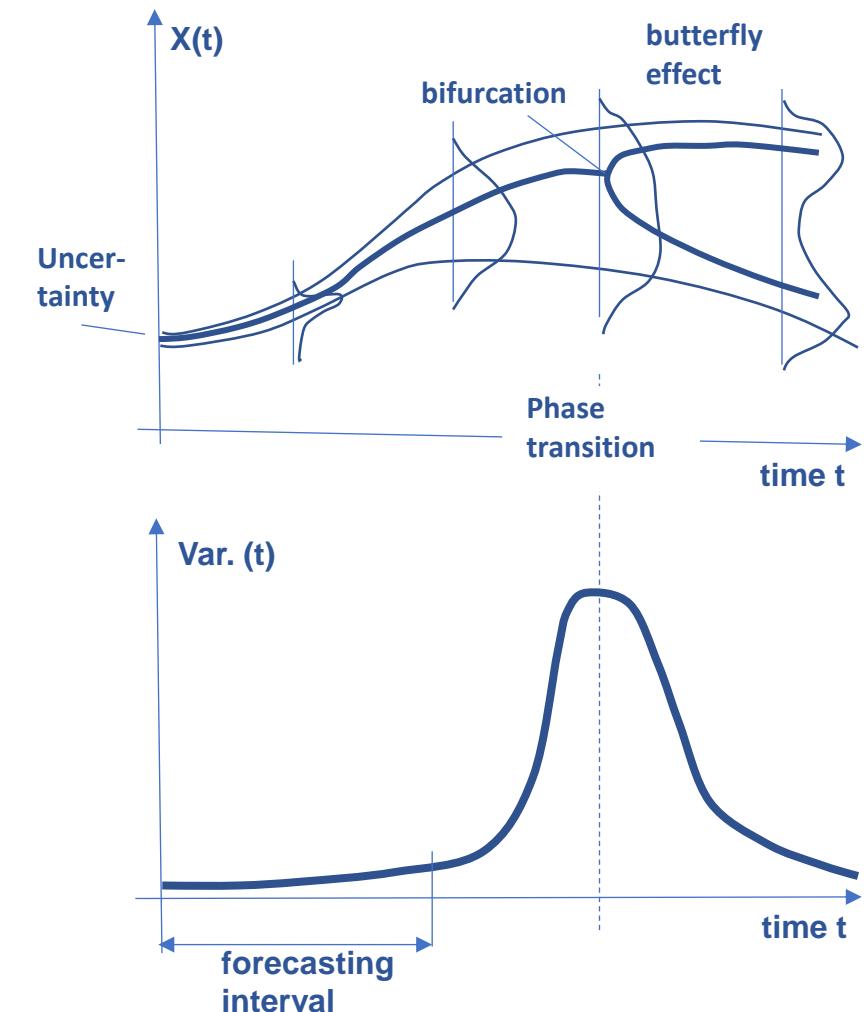
- non linearities in the system may create phase transitions
- new up to now unknown variables may appear (P. Allen)
- social systems are capable of learning unexpected events (Ukraine war)

## What can we do?

- scenarios technology - simulation of different possible events (best, expected, worst)
- simulation of uncertainties (Monte Carlo procedure, agent based modelling)

## Conclusion

- not only one trajectory but a bundle of trajectories
- length of forecasting period is limited



## Extended equations of motion, supply side dynamics included

Lecture Notes in Economics and Mathematical systems 369, Reiner Koblo, 1991

### investors configuration index

$$\frac{d\bar{x}(t)}{dt} = 2\nu[\sinh(\delta(t) + \kappa\bar{x}(t) + c_3w(t)) - \bar{x}(t)\cosh(\delta(t) + \kappa\bar{x}(t) + c_3w(t))]$$

### alternator dynamics

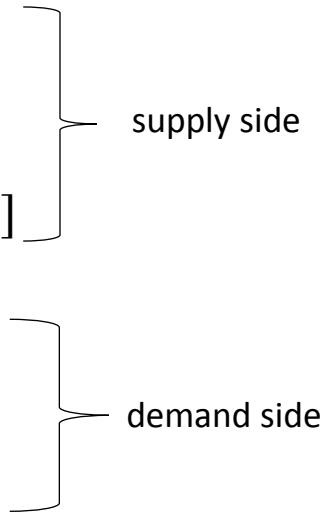
$$\frac{d\delta(t)}{dt} = -2\mu[\sinh(\beta\bar{x}(t) + c_4w(t) - \delta(t)Q) - \delta(t) \cosh(\beta\bar{x}(t) + c_4w(t) - \delta(t)Qt)]$$

### consumers configuration index

$$\frac{dw(t)}{dt} = -2\gamma[\sinh(c_1\delta(t)Q + c_2\bar{w}(t)) - q \cosh(c_1Q + c_2\bar{w}(t))]$$

strategic production  
propensity to consume

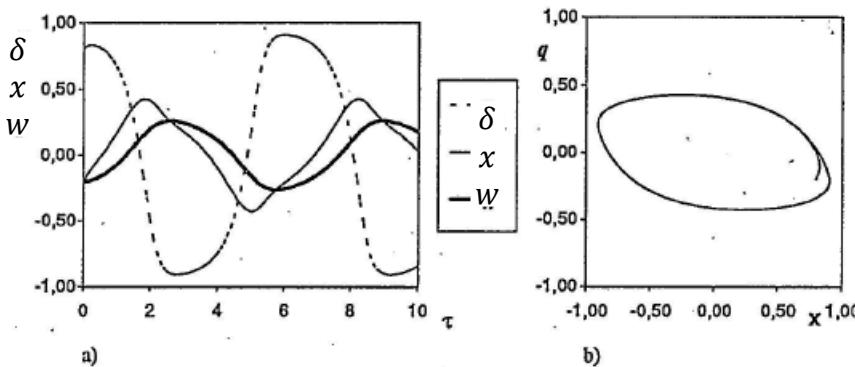
higher production level,  
→ higher income



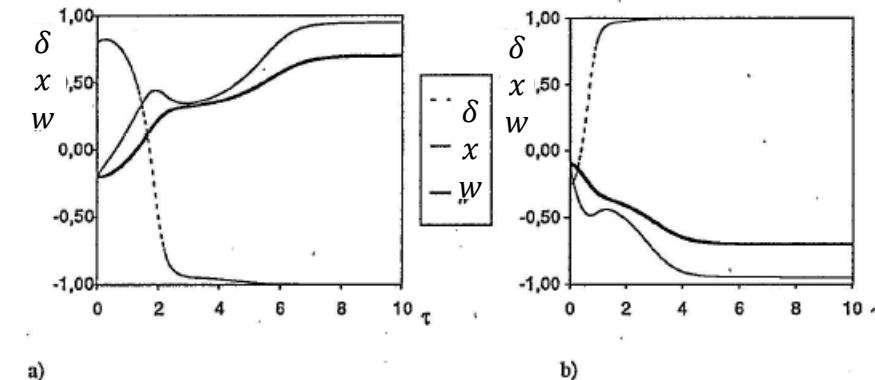
Static solutions, limit cycles, chaotic solutions (strange attractor)

# Selected Solutions of the extended Schumpeter Clock

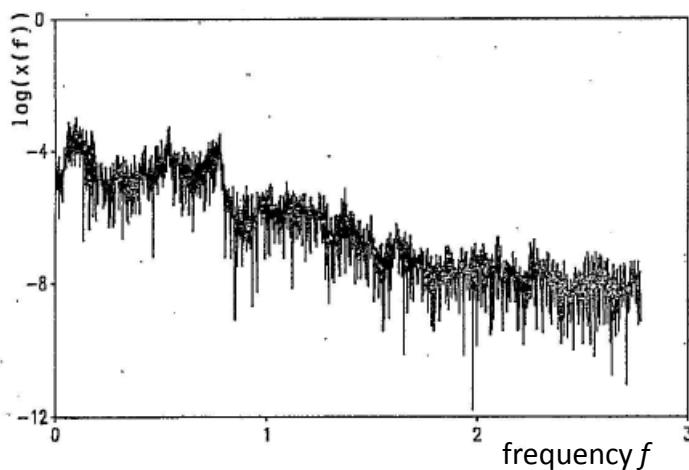
supply side and demand side



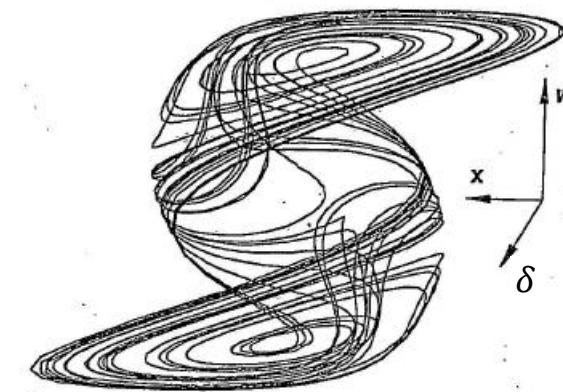
periodic solutions, limit cycle



one of many possible stationary solutions

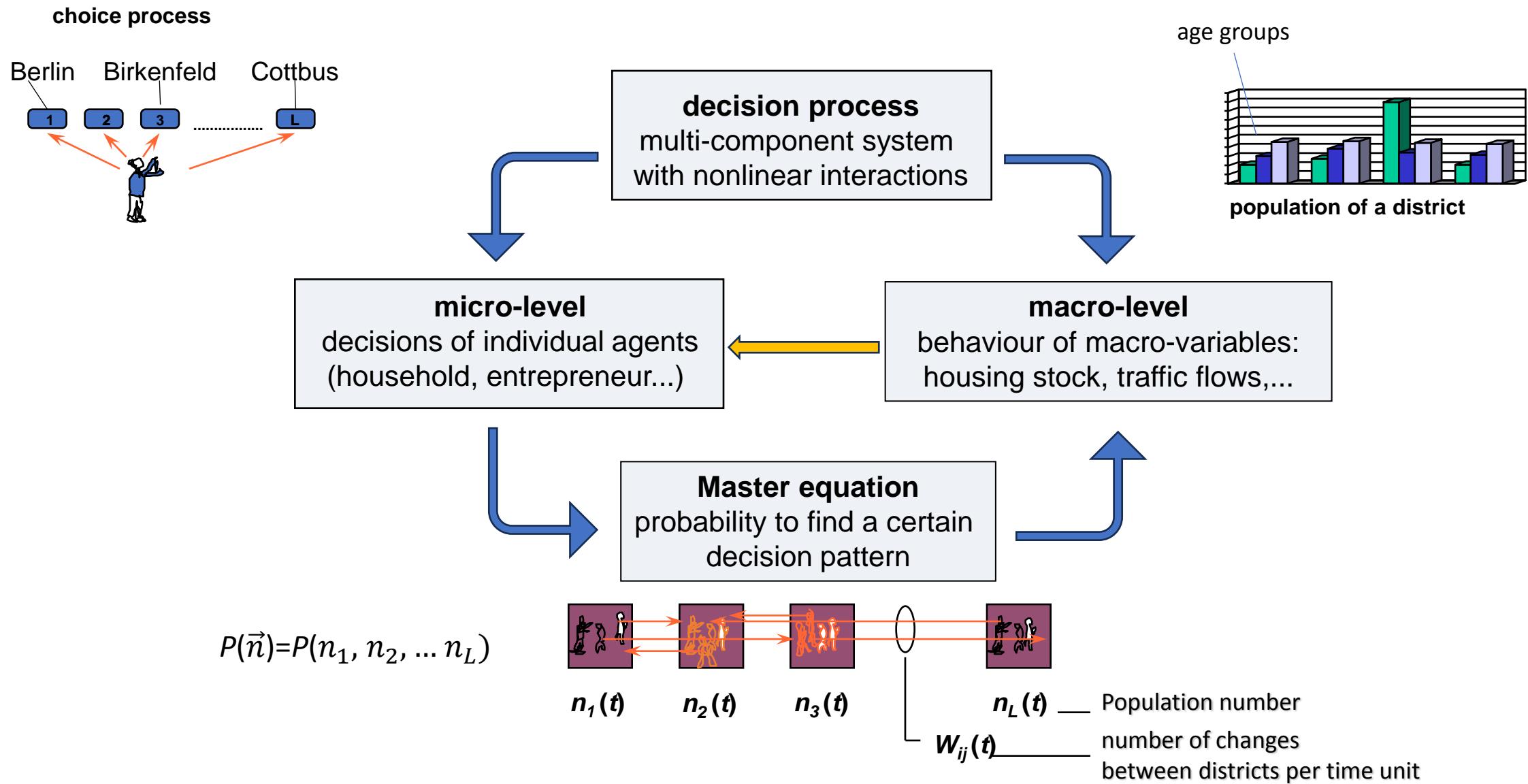


typical chaotic spectrum



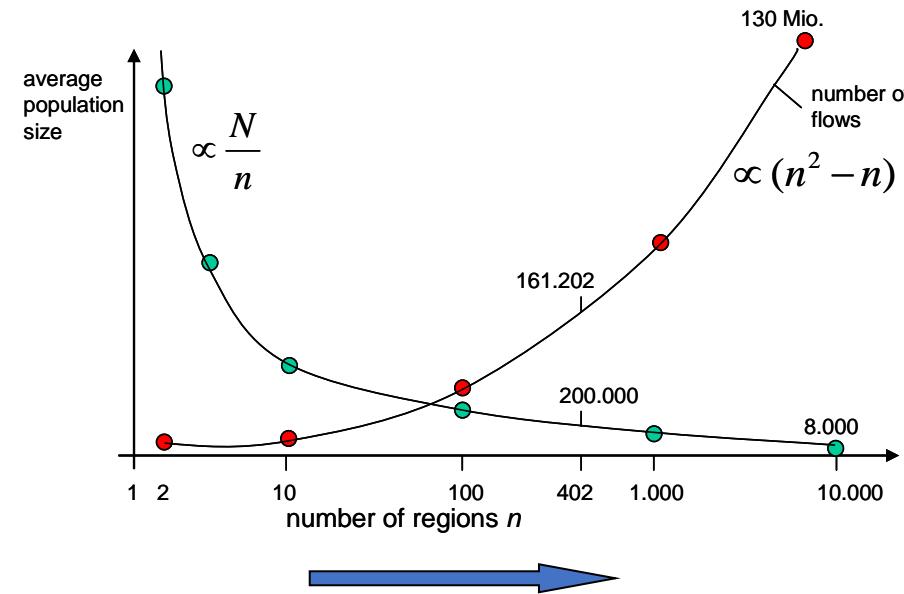
phase space of a strange attractor

## 2. Example: Interregional Migration (German districts and communes)



The smaller the spatial units the more interregional migration  
dominates the population dynamics

In Germany 400 districts and 10.994 communes (2021)



Increase of quality of the measure „distance“  
Increase of the number of zero flows

# How to construct the transition rates?

## transition rate: individual agents

$$w_{ij}(\vec{n}, t) = \sum_{\alpha} p_{ij}^{\alpha}(\vec{n}, \kappa, t)$$

sum over all agents  $\alpha$   
performing a transition

Assumptions concerning individual choice processes  
Information from panel data or surveys  
Master equation performs the averaging procedure

Computer performs the averaging



## transition rate: group specific

$$w_{ij}(\vec{n}, t) = n_i^{\gamma} p_{ij}^{\gamma}(\vec{n}, \kappa, t)$$

group index  
number of agents  
transition rate

**Master equation procedure**

**multi-agent-system (MAS)**

transition rate: changes of residence per year

$$w_{ij}(\vec{n}, t) = n_i p_{ij}(\vec{n}, \vec{\delta}) = n_i v_{ij} \exp(u_j(\vec{n}, \vec{\delta}) - u_i(\vec{n}, \vec{\delta})) \geq 0$$

change of residence  
 per time unit  $i$  to  $j$

population  
 living in  
 region  $i$

"individuel"  
 transition rate  
 from  $i$  to  $j$

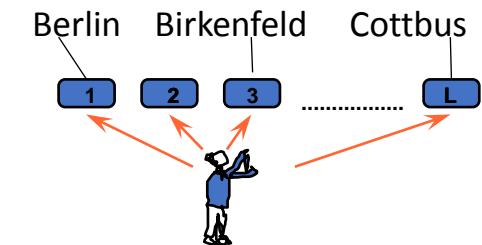
effect of „distance“  
 (symmetric matrix)

$v_{ij} = v_{ji}$

difference in spatial  
 attractiveness or utilities

concentration of information

choice process



regional attractiveness and spatial preferences

$$u_i = \kappa n_i + \delta_i(t)$$

regional  
 attractive-  
 ness

spatial  
 agglomeration  
 effect

regional  
 preference

$$\delta_i(t) = w_1 XW_i + w_2 XB_i + w_3 XV_i + w_4 XT_i + w_5 XF_i + w_6 XU_i$$

regional  
 preference

housing  
 market  
 indicator

services

accessibility  
 indicator

leisure time  
 Indicator

environment

## Exact stationary solution of the decision model master equation:

### exact stationary solution of the master equation

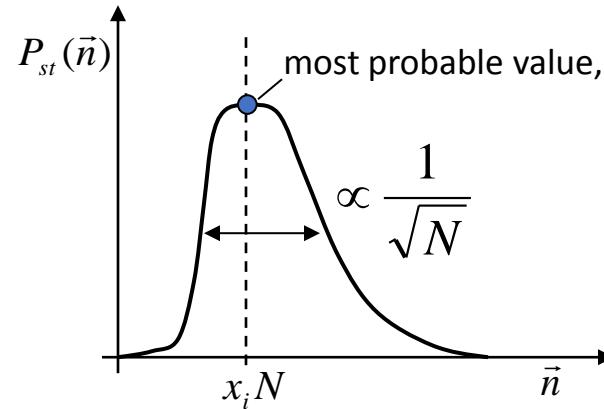
system fulfills detailed balance

$$P_{st}(\vec{n}) = \frac{Z^{-1} \delta\left(\sum_{i=1}^L n_i - N\right)}{n_1! n_2! \dots n_L!} \exp\left(2 \sum_{i=1}^L \sum_{m=1}^{n_i} u_i(m)\right)$$

Individuals are not  
distinguishable

most probable value,  
Stirling formula

$$\hat{x}_i = \frac{n_i}{N} = \frac{\exp(2u_i(\vec{x}))}{\sum_{j=1}^L \exp(2u_j(\vec{x}))}$$

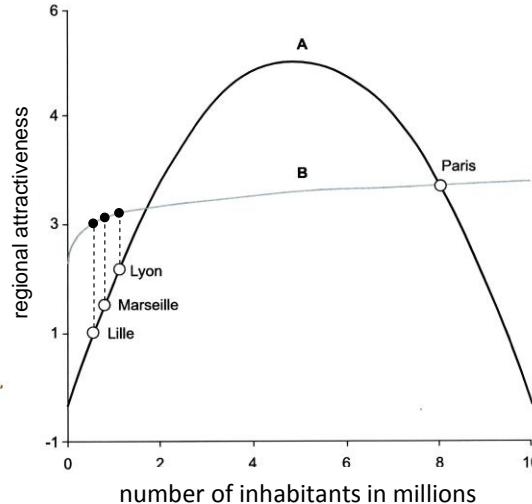


Environment fixed: system moves towards its equilibrium (10 to 20 years)  
 Policy changes environment: system always behind its equilibrium state

- MNL (multinomial logit model) most probable state for non-interacting individuals
- interactions between individuals (identity economics, Akerlof 1997)
- no memory effects included
- fixed number of alternatives

## Test of different size-effects of city attractiveness values

France system of 78 cities



### Hypothesis A

$$u_{kt} = \delta_{kt} + \kappa n_{kt} - \sigma n_{kt}^2$$

### Hypothesis B

$$u_{kt} = \delta_{kt} + \kappa \log n_{kt}$$

regional preference indicator

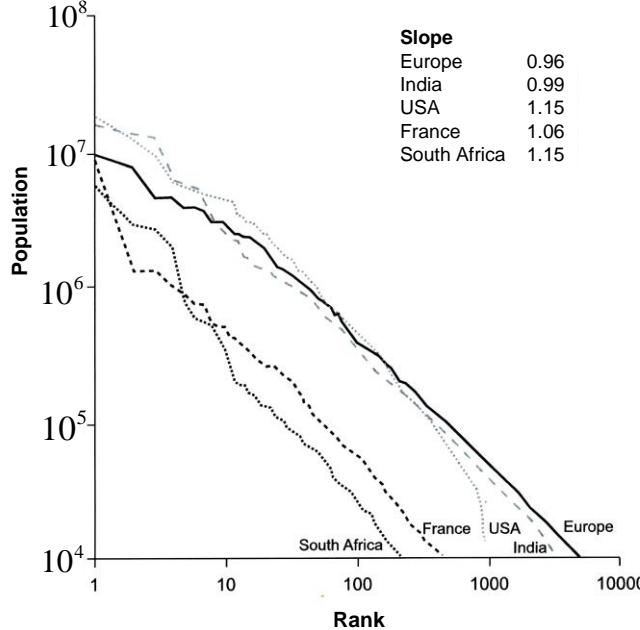
$$\delta_i = w_1 XW_i + w_2 XB_i + w_3 XV_i + w_4 XT_i + w_5 XF_i + w_6 XU_i$$

housing market indicator      employment indicator      services      accessibility indicator      leisure time indicator      environment

# Some fundamental considerations

**Zipf- distribution dominates in the long run**

Scaling relationship, self-similarity: reproduces itself on different scales



$$n_k = n_1 k^{-q}$$

population of city  $k$

Pareto coefficient

population of biggest city 1

rank of city  $k$

In the long run the migration model should produce a Zipf - distribution

$$\begin{aligned}
 \frac{d\langle n_j \rangle}{dt} &= \sum_{i=1}^L \langle n_i \rangle p_{ji}(\langle \vec{n} \rangle) - \sum_{i=1}^L \langle n_j \rangle p_{ij}(\langle \vec{n} \rangle) + \langle w_{j+} \rangle - \langle w_{j-} \rangle \\
 &= \sum_{i=1}^L v_{ji} \langle n_i \rangle \exp(u_j(\langle \vec{n} \rangle) - u_i(\langle \vec{n} \rangle)) - \sum_{i=1}^L v_{ij} \langle n_j \rangle \exp(u_i(\langle \vec{n} \rangle) - u_j(\langle \vec{n} \rangle)) + \rho_j(t) \langle n_j \rangle
 \end{aligned}$$

# Simulation of long-time development (France):

## Hypothesis A

$$u_k = \delta_k + \kappa n_k - \sigma n_k^2$$

attractivity      preference      agglomeration effect

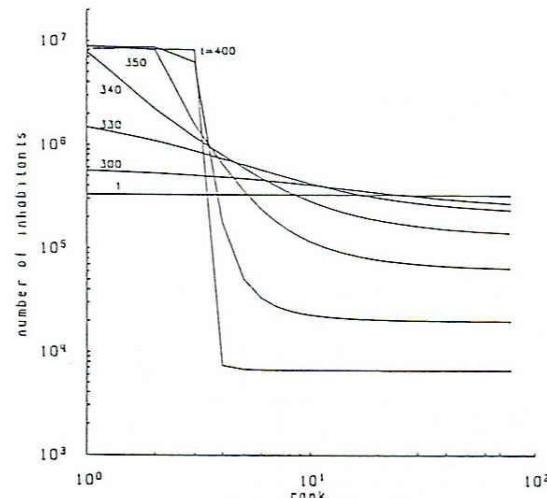


Figure 5 Simulation of an urban system using assumption A

$\kappa = 0.596$ ;  $\sigma = 0.188$ ;  $\nu = 0.001$ ;  $N = 25.6 * 10^6$ ;  $L = 78$ .

**some big cities, many small cities**

critical value       $K_c = \frac{1}{2} \frac{L}{N}$

## Hypothesis B

$$u_k = \delta_k + \kappa \log n_k$$

preference      agglomeration effect

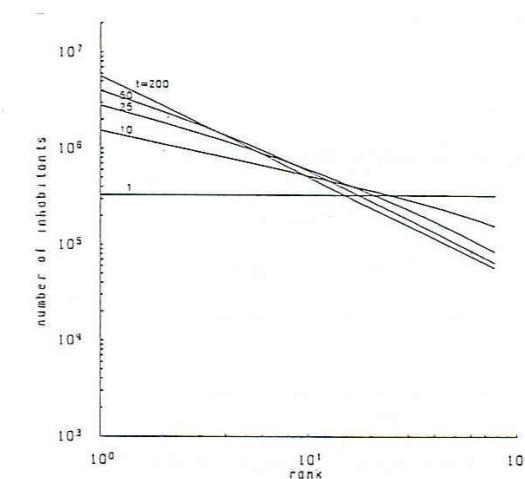


Figure 6 Simulation of an urban system using assumption B

$a = 0.500$ ;  $\nu = 0.001$ ;  $N = 25.6 * 10^6$ ;  $L = 78$ .

## Zipf-distribution (rank-size distribution)

critical value       $K_c = \frac{1}{2}$

Pareto coefficient       $q(t) = 2\kappa$

# The structure of the migration flow model (hypothesis B)

## Migration model

$$W_{ij} = n_i v_0 f_{ij} \exp( a \ln n_j - a \ln n_i + \delta_j - \delta_i )$$

$$W_{ij} = v_0 f_{ij} n_i^{(1-a)} n_j^a \exp(\delta_j - \delta_i)$$

regional preferences

for  $a > \frac{1}{2}$  destination area preferred

for  $a < \frac{1}{2}$  home area preferred

for  $a = \frac{1}{2}$  no preference for any region (SOC)

$$W_{ij} = v_0 f_{ij} \sqrt{n_i n_j} \exp( \delta_j - \delta_i )$$

mobility      regional interdependencies      population      difference of regional preferences

# Mobility and regional interdependencies

$$\nu_0 = \frac{1}{L(L-1)} \sum_{\substack{i,j=1 \\ i \neq j}}^L \nu_{ij}$$

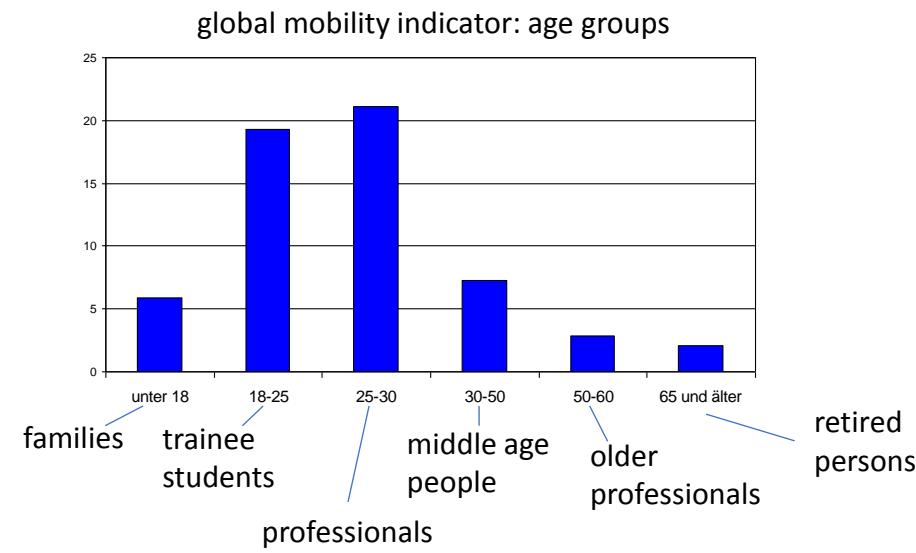
global mobility  
indicator

$$\nu_{ij} = \nu_0 f_{ij}$$

regional  
interdependencies

$$\frac{1}{L(L-1)} \sum_{\substack{i,j=1 \\ i \neq j}}^L f_{ij} = 1$$

normalization of regional  
interdependencies

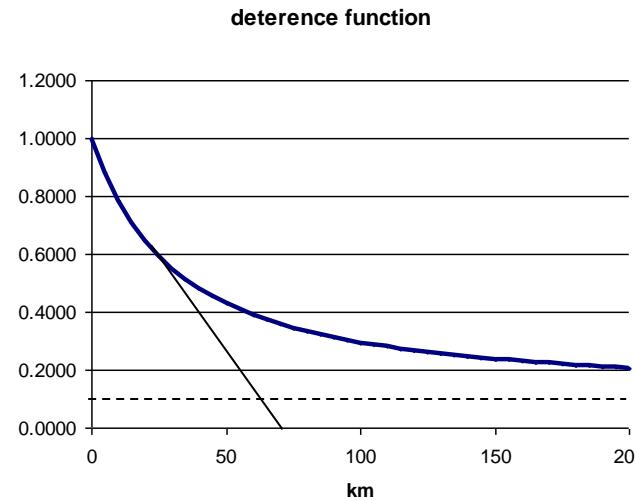


The effect of spatial distance  $d_{ij}$

$$f_{ij}(d_{ij}) = \exp\left(-\frac{\beta d_{ij}}{1 + \gamma d_{ij}}\right)$$



$\beta ; \gamma$

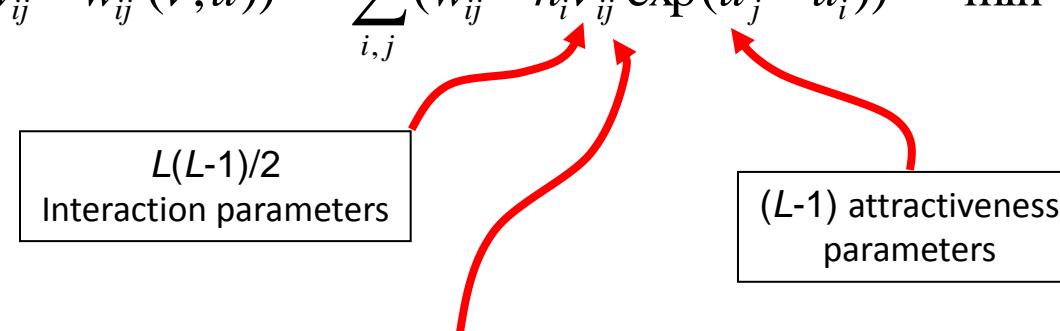


## empirical data base

$$(n_i^e(t), w_{ij}^e(t)) \quad \text{for } i, j = 1, 2, \dots, L \quad \text{and } i \neq j$$

## parameter estimation via cost function\*

$$F[\nu, \vec{u}] = \sum_{i,j} (w_{ij}^e - w_{ij}^m(\nu, \vec{u}))^2 = \sum_{i,j} (w_{ij}^e - n_i \nu_{ij} \exp(u_j - u_i))^2 = \min$$


 L(L-1)/2  
 Interaction parameters

(L-1)  
 attractiveness  
 parameters

$$\text{or } \nu_{ij}(d_{ij}) = \nu_0 \exp\left(-\frac{\beta d_{ij}}{1 + \gamma d_{ij}}\right)$$

(161.202 flows, 80.601 interaction parameters and 401 attractiveness parameters  
 in case of German districts)

Ratio: number of data / number of parameters: **2/1 ??!!**

### empirical data base

$$(n_i^e(t), w_{ij}^e(t)) \quad \text{for } i, j = 1, 2, \dots, L \quad \text{and } i \neq j$$

### parameter estimation via cost function

$$F[\nu, \vec{u}] = \sum_{i,j} (w_{ij}^e - w_{ij}^m(\nu, \vec{u}))^2 = \sum_{i,j} (w_{ij}^e - n_i \nu_{ij} \exp(u_j - u_i))^2 = \min$$

or

$$\delta F(\underline{\nu}, \vec{u}) = \sum_{i=1}^L \left[ \frac{\partial F}{\partial u_i} + \lambda \right] \delta u_i + \frac{1}{2} \sum_{\substack{i,j \\ i \neq j}}^L \left[ \frac{\partial F}{\partial \nu_{ij}} + \frac{\partial F}{\partial \nu_{ji}} \right] \delta \nu_{ij} = 0 \quad \text{with constraint} \quad \sum_{i=1}^L u_i = 0$$

This leads to the equations

$$\frac{\partial F}{\partial u_i} + \lambda \xrightarrow{\text{Lagrange parameter}} 0 \quad \text{for } i = 1, 2, \dots, L$$

$$\frac{\partial F}{\partial \nu_{ij}} + \frac{\partial F}{\partial \nu_{ji}} = 0 \quad \text{for } i, j = 1, 2, \dots, L \quad \text{with } i \neq j$$

## estimation of attractiveness and regional interdependencies

complete migration matrix available (402 districts in Germany)

### principle of minimizing errors

$$F[\vec{u}, v_{ij}] = \sum_{i,j} (w_{ij}^e - w_{ij}^m(\vec{u}, v_{ij}))^2 = \sum_{i,j} (w_{ij}^e - n_i^e v_{ij} \exp(u_j - u_i))^2 \stackrel{!}{=} \min$$

$$\frac{\partial F}{\partial v_{ij}} + \frac{\partial F}{\partial v_{ji}} = 0$$

$$v_{ij} = \frac{n_j^e w_{ij}^e \exp(u_i - u_j) + n_i^e w_{ji}^e \exp(u_j - u_i)}{n_j^{2,e} \exp(2(u_i - u_j)) + n_i^{2,e} \exp(2(u_j - u_i))} = v_{ji}$$

attractiveness  
indicators

→

regional  
interdependencies

Interaction term completely determined by attractiveness values and empirical data

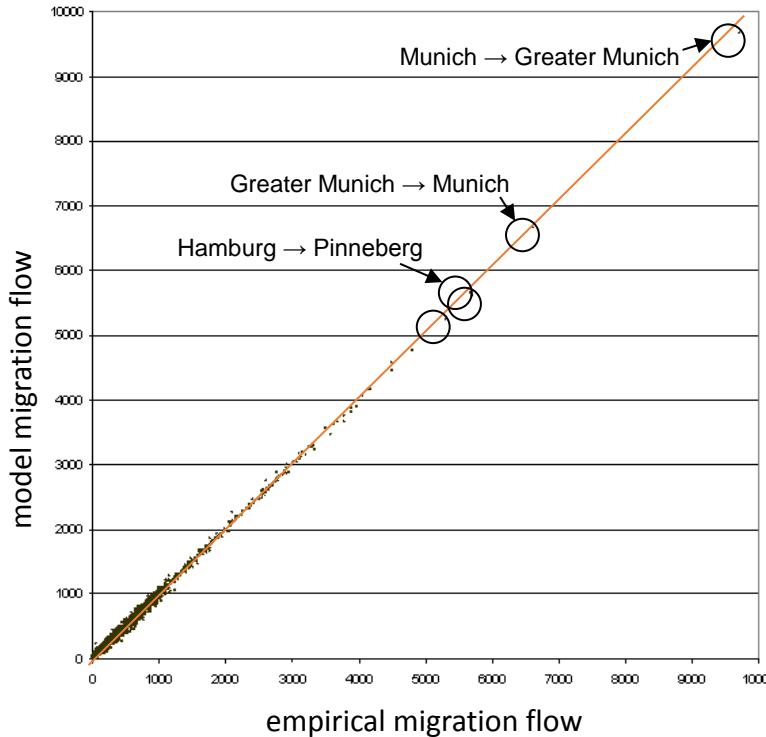
$(L^2-L)$  migration data,  $(L-1)$  attractiveness parameters have to be determined,  
 (161.202 flows, 401 attractiveness parameters in case of German districts)

Ratio: number of data / number of parameters: 402/1

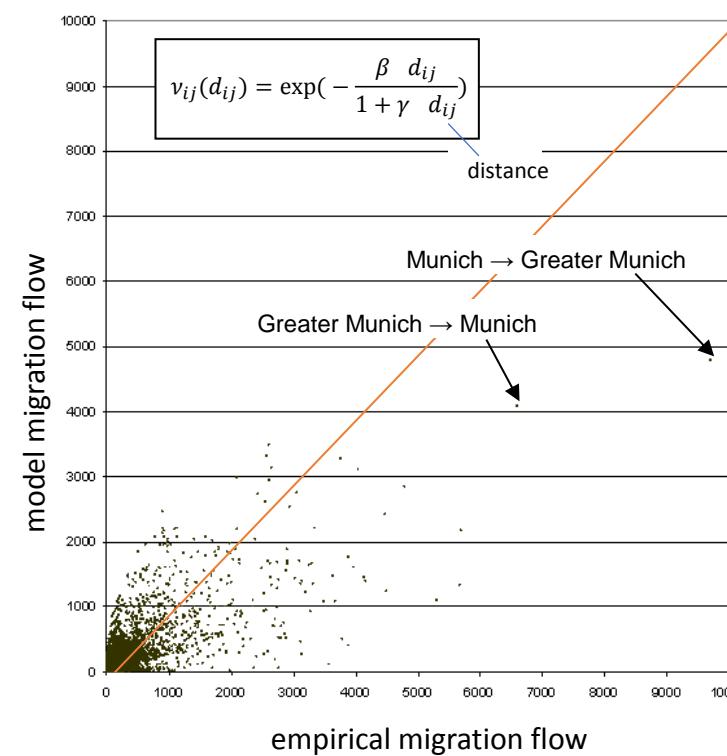
## parameter estimation via cost function\*

$$F[v, \vec{u}] = \sum_{i,j} (w_{ij}^e - w_{ij}^m(v, \vec{u}))^2 = \min \quad \longrightarrow \text{all trend parameters}$$

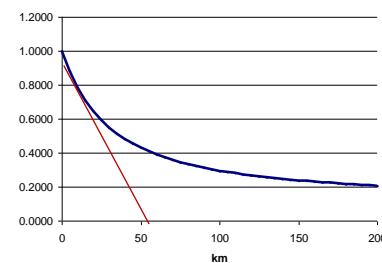
estimated spatial interaction term



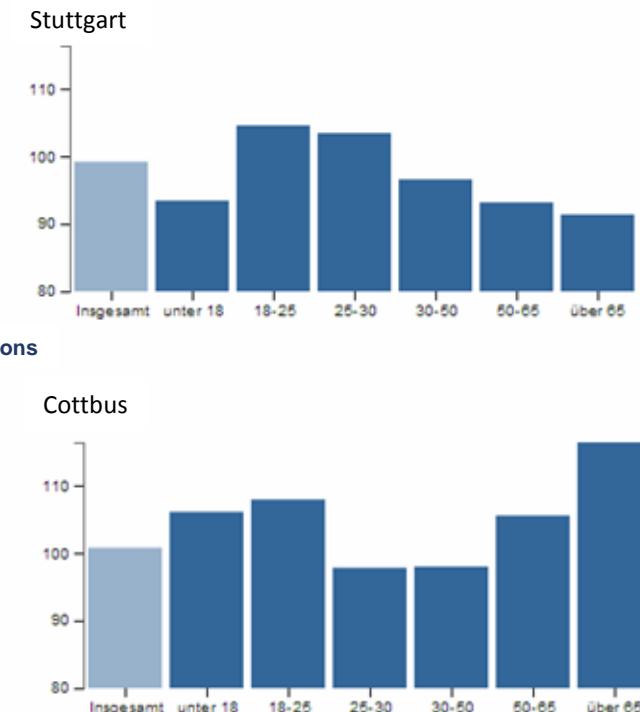
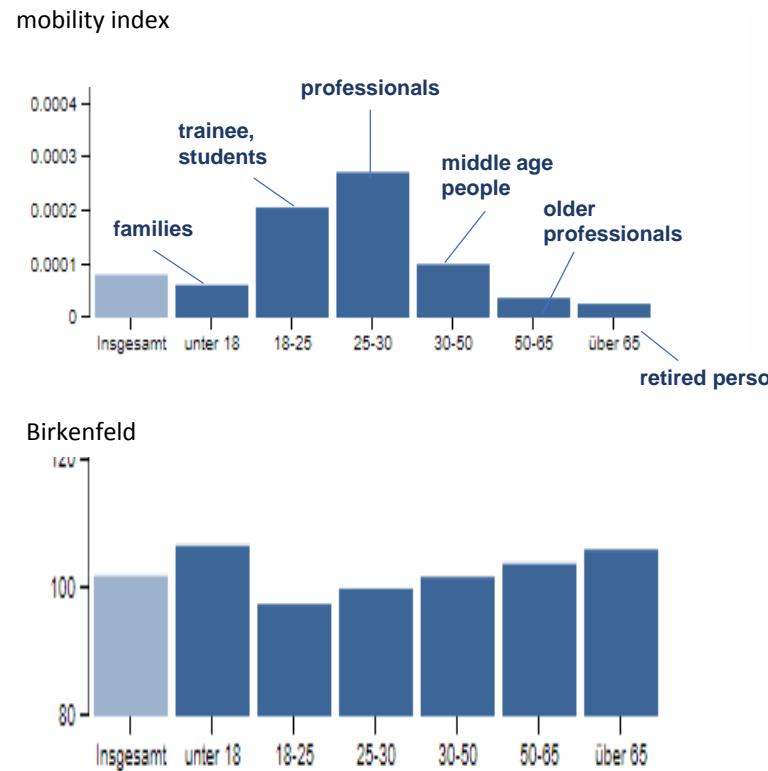
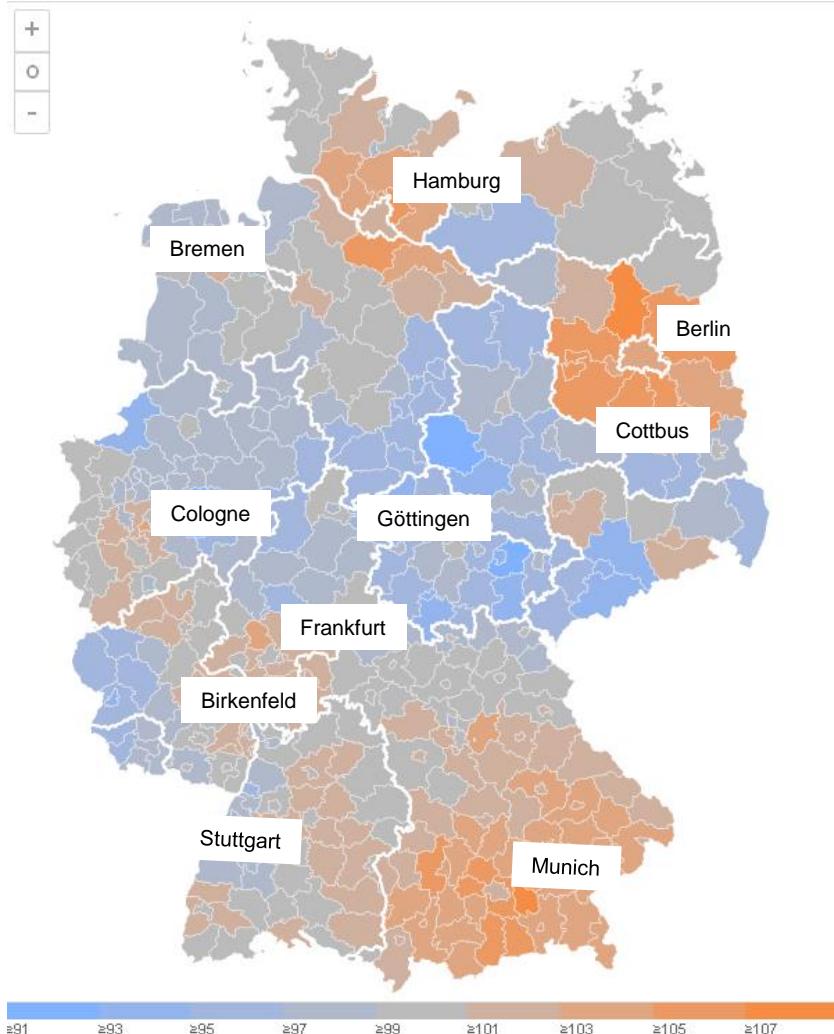
assumed distance dependence



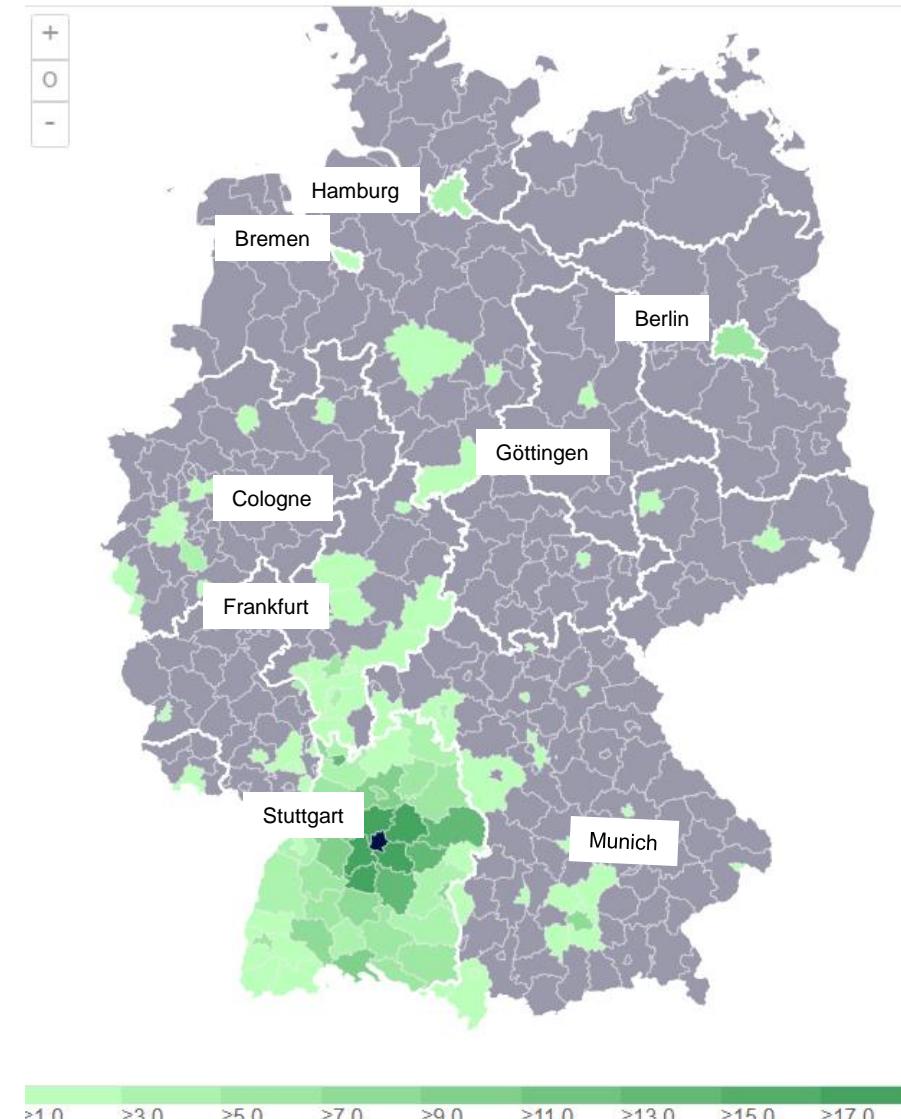
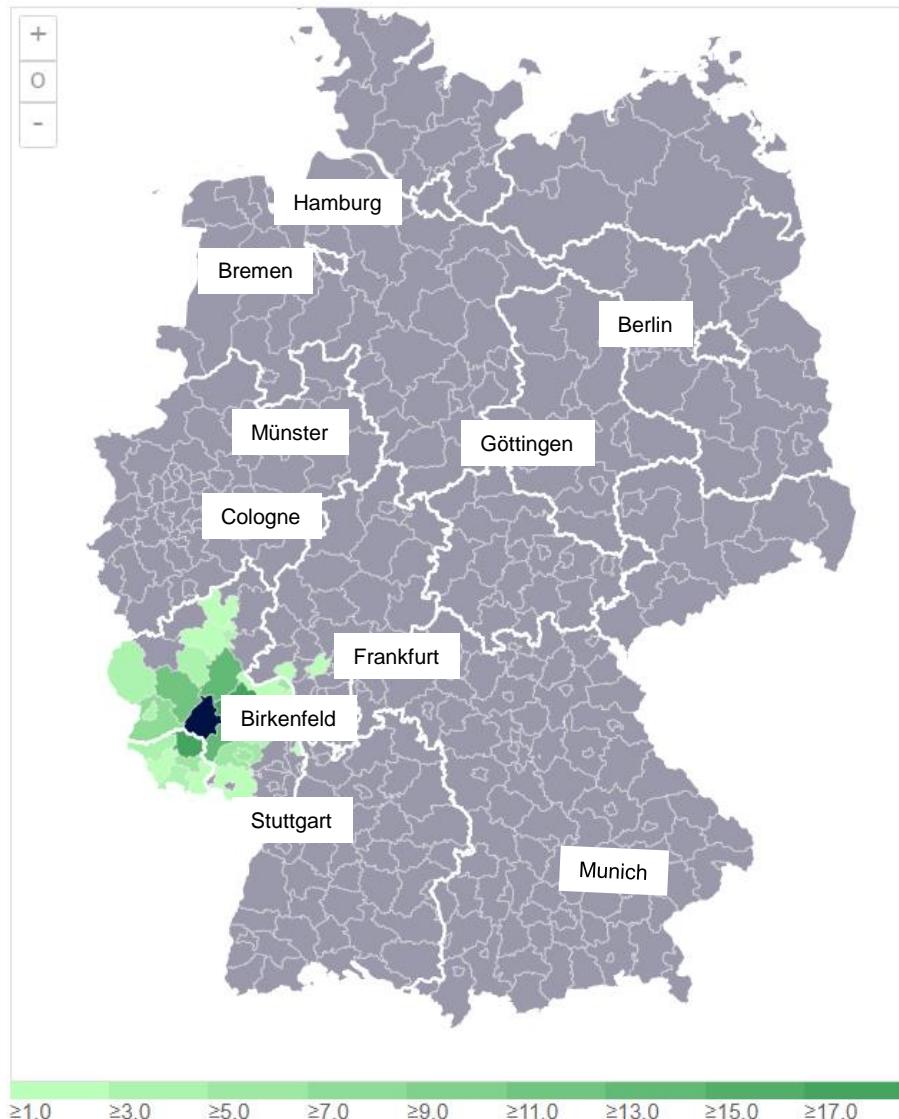
distance function



# Spatial preferences (total population): districts (400)



# Strength of spatial interaction: City of Birkenfeld (left) and Stuttgart (right) with other districts



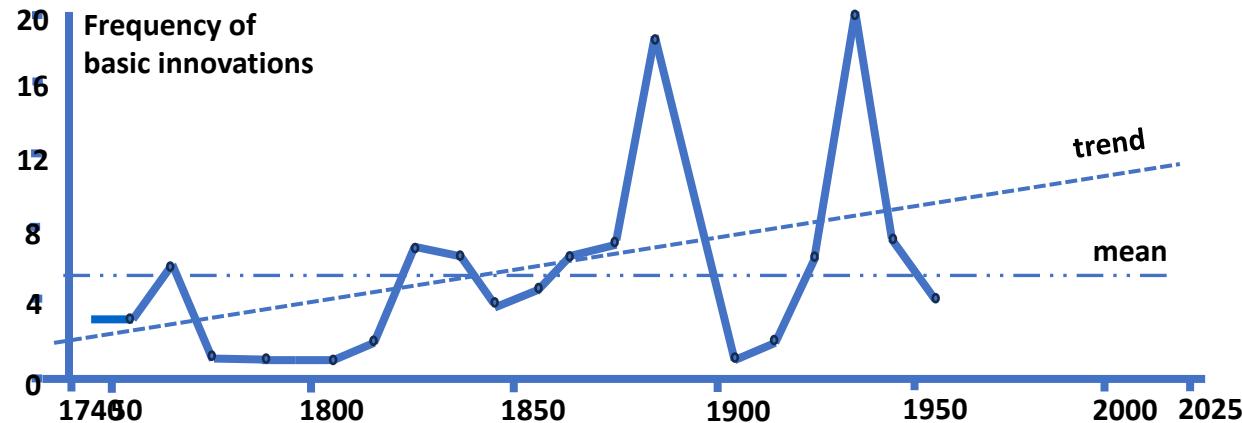
Presentation of German interaction data  
Level of districts and communities

# Regression analysis of regional preferences

Variables	Model 1	Model 2	Model 3
Const.	-0.680*** (-10.044)	-0.142*** (-2.935)	-0.040 (-0.667)
GfK	2.406E-5*** (8.609)		
NDW	0.009*** (4.955)		
SB	0.014* (1.898)	0.026*** (3.587)	0.036*** (4.644)
ALQ		-0.003 (-1.383)	-0.008*** (-2.649)
BLS		1.784E-6* (1.500)	1.603E-6 (1.132)
CP		0.016*** (8.252)	
PD			0.001*** (3.154)
TCAR			-0.001 (-0.464)
R <sup>2</sup> ad	0.346	0.283	0.179

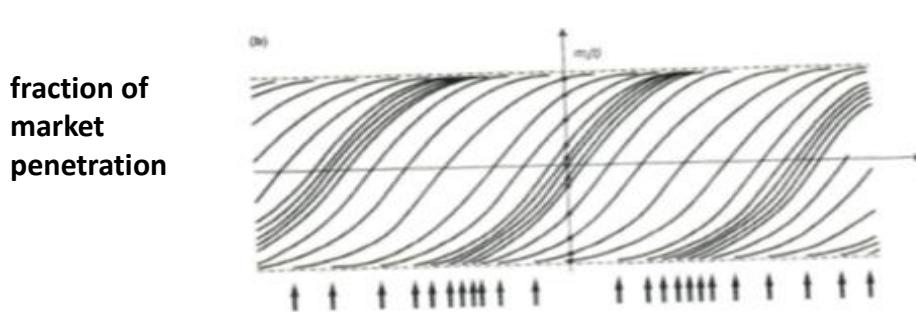
Note: Values in parenthesis are t-values. \*\*\*, \*\*, and \* indicate the significance levels at the 1, 5, and 10 % using t-statistic. GfK = available income per capita, NDW = new dwellings per 1000 existing dwellings, SB = shop balance: number of business openings and closings per 1000 capita, ALQ = rate of unemployment, BLS = income per capita, CP = construction permit per 1000 existing dwellings, PD = patent density: patents per 1000 capita, TCAR = travel time per car to the next highway

### 3. Example: Basic Innovations, G. Mensch



G. Mensch (1979): Stalemate in Technology, Frequency of basic innovations, 1740 – 1960.

The numbers of basic innovations reported here are given in 10 years bunches.



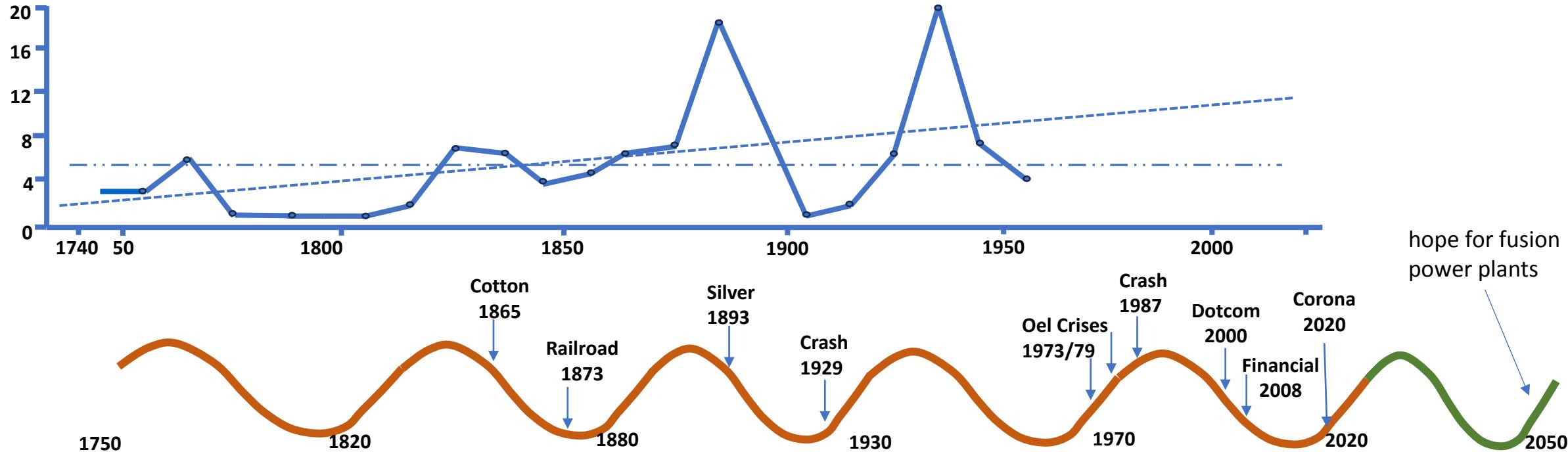
#### Basic innovations

- Clustering of Innovations, G. Mensch
- Basic innovations give rise to a new industry

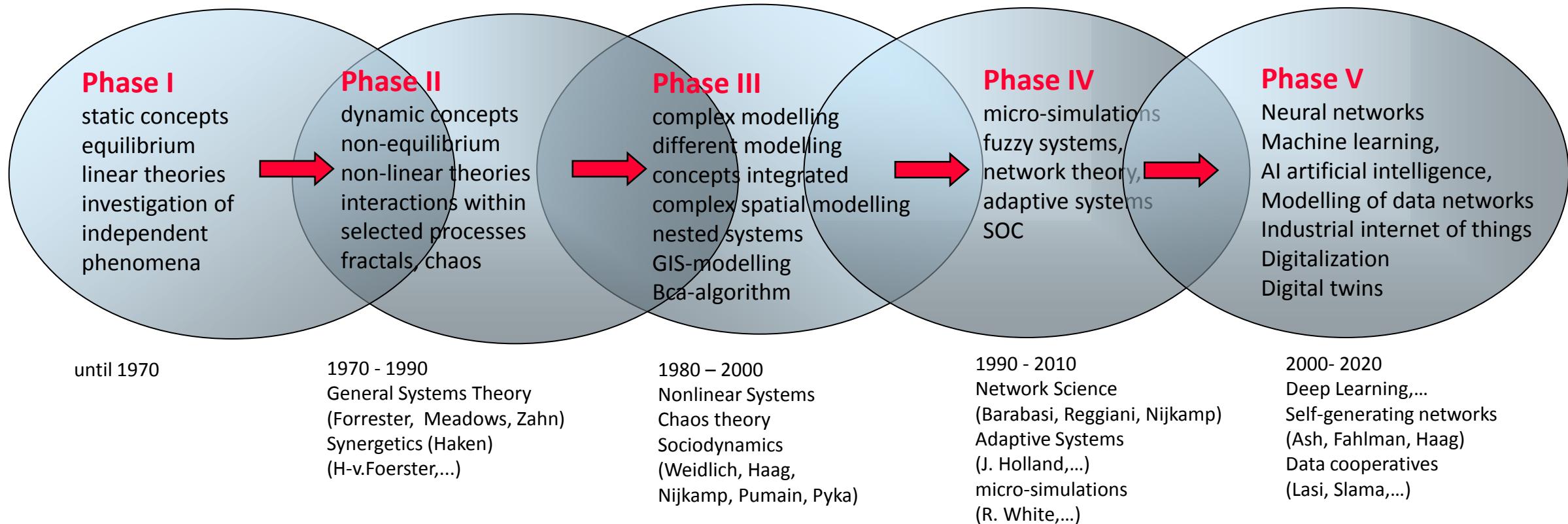
#### Long-term economic cycles

- Cycle time 40 to 60 years, Cesare Marchetti (54 years, energy sector)
- Logistic growth curve of technologies
- If a technology enters its peak → chance for a new technological breakthrough (e.g. coal → oil → gas → nuclear → green)

# Basic Innovations and Long Waves



	Kondratieff 1	Kondratieff 2	Kondratieff 3	Kondratieff 4	Kondratieff 5	Kondratieff 6
	Dampfmaschine, Textilindustrie, Eisenproduktion, Mechanisierung der Produktion	Eisenbahn, Stahl, Schwer- industrie, Dampfschiffe, Brücken- und Bahnhöfe, Vernetzung über die Schiene	Chemie, Elektroindustrie, Elektrizität, Elektrogeräte, Röhrentechnik	Automobil, Petrochemie Kerntechnik, Transistor, Radio, Fernseher, Kühlschrank, PC- Computer, Zuse Z3	Computertechnik, PCs, Informationstech. Halbleitertechnik, Internet, Smartphone, GPS, integrierte Bau- teile,	Grüne Energie, KI, Elektrofahrzeuge, Biotechnologie, vegane Ernährung, Blockchain, ChatGPT, Wasserstoff, Sustainable products
	<b>1. Industrielle Revolution</b>		<b>2. Industrielle Revolution</b>		<b>3. Ind. Rev.</b>	<b>4. Ind. Rev., 5. Rev.</b>



The ideas of H. v. Foerster, H. Haken, W. Weidlich, Prigogine and other pioneers survive and will foster new developments in the scientific society

The theories and tools currently available make research more effective and support interdisciplinary research

**Thank You for your attention**